# Year 4 Arithmetic Workbook

by Richard Brown

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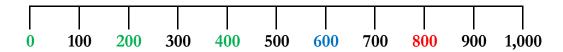
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# **Key Language and Representations**

**Word Problems** are the arithmetic number sentences written in a real-life reasoning and problem solving scenario.

**Concrete Objects** are manipulated or handled to calculate and represent a number sentence i.e. counters, multilink cubes, fraction tiles, metric rulers.

**Metric Ruler** used to count forwards e.g. 0, 6, 12, 18, 24, 30 and also to count backwards e.g. 54, 45, 36, 27, 18, 9.



**Column Addition** is the formal written method of adding two or more numbers together, using a vertical arrangement in a columnar format, with regrouping.

**Column Subtraction** is the formal written method of subtracting a smaller number from a bigger number, using a vertical arrangement in a columnar format, with regrouping.

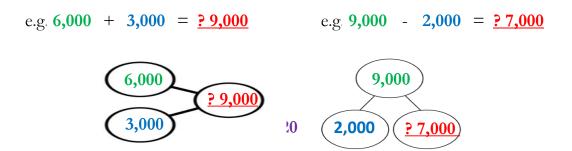
1 000

100

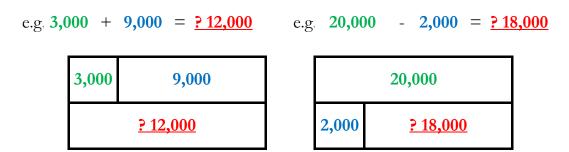
		<u>1,000s</u>	<u>100</u>	<u>s 10s</u>	<u>1s</u>
<u>10s</u> <u>1s</u>	<u>1,000s</u> <u>100s</u> <u>10s</u> <u>1s</u>				
	4,000 70		5	9	
1 5	<del>5,000</del> <sup>1</sup> 700 <del>80</del> <sup>1</sup> 5	9	6	<b>1</b> 0	<b>1</b> 4
- 4 -	2,000 900 40 6	-	3	9	4
1 1	2,000 800 30 9	9	2	0	6

**Strategy Applied** refers to when a formal written method is used to calculate a number sentence e.g. 30,250 - 5,000 = 25,250 Explained using appropriate mathematical language, proven using concrete objects that can be handled, shown with pictorial representations visualising the calculations, to ensure a greater understanding of a mathematical concept.

Part Whole Models are pictorial mathematical images to represent varied calculations and number sentences.

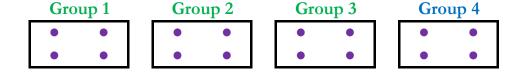


Bar Models are an image, that pictorially represents a number sentence.



**Groups of objects** represents a total number of objects shared or divided into two or more groups of an equal number of the objects.

$$\frac{3}{4}$$
 of 1,600 = 1,200 • represents the value of 100



# Number Grid

0	1	2	3	4	5	6	7	8	9
10	11	12	13	14	15	16	17	18	19
20	21	22	23	24	25	26	27	28	29
30	31	32	33	34	35	36	37	38	39
40	41	42	43	44	45	46	47	48	49
50	51	52	53	54	55	56	57	58	59
60	61	62	63	64	65	66	67	68	69
70	71	72	73	74	75	76	77	78	79
80	81	82	83	84	85	86	87	88	89
90	91	92	93	94	95	96	97	98	99
100	101	102	103	104	105	106	107	108	109
110	111	112	113	114	115	116	117	118	119
120	121	122	123	124	125	126	127	128	129
130	131	132	133	134	135	136	137	138	139
140	141	142	143	144	145	146	147	148	149
150	151	152	153	154	155	156	157	158	159

# <u>Multiplication Square</u>

x	2	3	4	5	6	7	8	9	10
0	0	0	0	0	0	0	0	0	0
1	2	3	4	5	6	7	8	9	10
2	4	6	8	10	12	14	16	18	20
3	6	9	12	15	18	21	24	27	30
4	8	12	16	20	24	28	32	36	40
5	10	15	20	25	30	35	40	45	50
6	12	18	24	30	36	42	48	54	60
7	14	21	28	35	42	49	56	63	70
8	16	24	32	40	48	56	64	72	80
9	18	27	36	45	54	63	72	81	90
10	20	30	40	50	60	70	80	90	100
11	22	33	44	55	66	77	88	99	110
12	24	36	48	60	72	84	96	108	120

# Decimal Number Grid

0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
1.0	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9
2.0	2.1	2.2	2.3	2.4	2.5	2.6	2.7	2.8	2.9
3.0	3.1	3.2	3.3	3.4	3.5	3.6	3.7	3.8	3.9
4.0	4.1	4.2	4.3	4.4	4.5	4.6	4.7	4.8	4.9
5.0	5.1	5.2	5.3	5.4	5.5	5.6	5.7	5.8	5.9
6.0	6.1	6.2	6.3	6.4	6.5	6.6	6.7	6.8	6.9
7.0	7.1	7.2	7.3	7.4	7.5	7.6	7.7	7.8	7.9
8.0	8.1	8.2	8.3	8.4	8.5	8.6	8.7	8.8	8.9
9.0	9.1	9.2	9.3	9.4	9.5	9.6	9.7	9.8	9.9
10.0	10.1	10.2	10.3	10.4	10.5	10.6	10.7	10.8	10.9
11.0	11.1	11.2	11.3	11.4	11.5	11.6	11.7	11.8	11.9
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9
13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9
14.0	14.1	14.2	14.3	14.4	14.5	14.6	14.7	14.8	14.9
15.0	15.1	15.2	15.3	15.4	15.5	15.6	15.7	15.8	15.9

# **Fraction Walls**

	1 Whole														
	$\frac{1}{2}$ $\frac{1}{2}$														
	$\begin{array}{c c} 1 \\ \hline 4 \end{array} \qquad \begin{array}{c c} 1 \\ \hline 4 \end{array}$									1 1	i			1 4	i
-	1	1	1	1	1	-	1	1	1	1	l	1	1	1	l
8	8 8 8 8							8	3	8	3	8	3	8	3
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
16	16	16	16	16	16 16 16 16				16	16	16	16	16	16	16

	1 Whole								
	1 2			1 2					
	<u>1</u> 3		<u>1</u> 3		<u>1</u> 3				
<u>1</u> 6	<u>1</u> 6	<u>1</u> 6	<u>1</u> 6	<u>1</u> 6	<u>1</u> 6				

	1 Whole																		
	$\frac{1}{2}$																		
	$\begin{array}{c c c c c c c c c c c c c c c c c c c $																		
	1		1	1	1	1	1		1		1		1		1		1	1	1
1	10 10 10 10 10 10								0	1	0	1	0	1	0	1	0		
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20

# **How Many**

How many **1,000s** (thousands), **100s** (hundreds), **10s** (tens), **1s** (ones), **10ths** (tenths) and **100ths** (hundredths) are there in the number **1,234.56**?

1) 1 2 3 4 . 5 6 =

#### Word Problem

The number one thousand, two hundred and thirty four point five six is a 6-digit decimal number.

The digits represent the following column place values the 1,000s, 100s, 10s, 1s, 10ths and 100ths.

Work out how many 1,000s, 100s, 10s, 1s, 10ths and 100ths, there are in each column.

#### **Strategy Applied**

On a **Place Value Grid** show the number **one thousand**, **two hundred** and thirty four point five six.

- 1 represents how many thousands in the 1,000s column place value.
- 2 represents how many hundreds in the 100s column place value.
- 3 represents how many tens in the 10s column place value.
- 4 represents how many ones in the 1s column place value.
- 5 represents how many tenths in the 10ths column place value.
- 6 represents how many hundredths in the 100ths column place value.

First, write 1 in the 1,000s column, the amount of thousands.

Then, write 2 in the 100s column, the amount of hundreds.

Next, write 3 in the 10s column, the amount of tens.

Then, write 4 in the 1s column, the amount of ones.

Next, write 5 in the 10ths column, the amount of tenths.

Then, write 6 in the 100ths column, the amount of hundredths.

Finally, there are 1 thousands, 2 hundreds, 3 tens, 4 ones, 5 tenths and 6 hundredths.

# Place Value Grid

<u>1000s</u>	<u>100s</u>	<u>10s</u>	<u>1s</u>	•	<u>10ths</u>	<u>100ths</u>
1	2	3	4	•	5	6

# **Test Questions**

How many **1,000s** (thousands), **100s** (hundreds), **10s** (tens), **1s** (ones), **10ths** (tenths) and **100ths** (hundredths) in each number?

# Digit Value

What is the digit value of the **1,000s** (thousands), **100s** (hundreds), **10s** (tens), **1s** (ones), **10ths** (tenths) and **100ths** (hundredths) in the number **1,234.56**?

#### Word Problem

The number one thousand, two hundred and thirty four point five six is a 6-digit decimal number.

Each digit represents the 1s, 10s, 100s and 1,000s column place values. What is the digit value of each digit in the number one thousand and two hundred and thirty four point five six?

### **Strategy Applied**

On a **Place Value Grid** show the number **one thousand, two hundred** and thirty four.

The 6 represents the digit value of the hundredths in the 100ths column.

The 5 represents the digit value of the **tenths** in the **10ths** column.

The 4 represents the digit value of the **ones** in the **1s** column.

The 3 represents the digit value of the tens in the 10s column.

The 2 represents the digit value of the hundreds in the 100s column.

The 1 represents the digit value of the thousands in the 1,000s column.

First, write 0.06 in the 100ths column, the value of the hundredths.

Then, write 0.5 in the 10ths column, the value of the tenths.

Next, write 4 in the 1s column, the value of the ones.

Then, write 30 in the 10s column, the value of the tens.

Next, write 200 in the 100s column, the value of the hundreds.

Then, write 1,000 in the 1,000s column, the value of the thousands.

Finally, the **Place Value Grid shows** the digit value of each of the digits as

1,000 200, 30, 4, 0.5, 0.06,

# Place Value Grid

<u>1000s</u>	<u>100s</u>	<u>10s</u>	<u>1s</u>	•	<u>10ths</u>	<u>100ths</u>
1,000	200	30	4	•	0.5	0.06

# **Test Questions**

What is the digit value of the **1,000s** (thousands), **100s** (hundreds), **10s** (tens), **1s** (ones), **10ths** (tenths) and **100ths** (hundredths) in each number?

- 1) 1,234.56 = \_\_\_\_
- 2) 1,246.19 = \_\_\_\_
- 3) 2,179.83 = \_\_\_\_
- 4) 3,537.74 =
- 5) 4,068.61 = \_\_\_\_
- 6) 5,379.02 = \_\_\_\_
- 7) 6,513.93 = \_\_\_\_
- 8) 7,215.48 = \_\_\_\_
- 9) 8,346.57 =
- 10) 9,537.20 = \_\_\_\_

# **1,000** more

#### Word Problem

Susan is thinking of a number. Her number is **one thousand more than one thousand, seven hundred and fifty**.

What is her number?

#### **Partitioning**

#### **Column Addition**

#### **Strategy Applied**

Partition both numbers into 1,000s, 10s, 1s and add together their relative digit values.

1,750 = 1,000 + 700 + 50 + 0 and 1,000 = 1,000 + 0 + 0 + 0.

First, add the **1,000s** digit values of **one thousand** and **one thousand**, equal to **two thousand**.

Then, add the **100s** digit values of **seven hundred** and **zero**, equal to **seven hundred**.

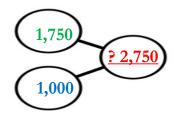
Next, add the 10s digit values of fifty and zero, equal to fifty.

Then, add the 1s digit values of zero and zero, equal to zero.

Next, use column addition to add the values of 2,000+700+50+0=2,750.

Finally, **1,750** plus **1,000** equals **2,750**.

#### Part Whole Model



#### **Test Questions**

#### **Bar Model**

1,750 1,000 ? 2,750

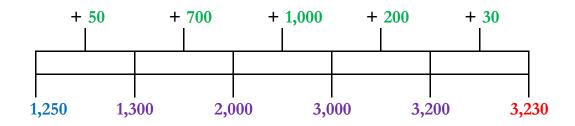
# More Than 1,000

#### Word Problem

London to Warsaw is three thousand, two hundred and thirty miles. Paris to Warsaw is one thousand, two hundred and fifty miles.

What is the **distance** from London to Paris?

#### Number Line



#### **Strategy Applied**

A number grid or a ruler can be used to **count on**.

First, draw a number line and write one thousand, two hundred and fifty at the start and three thousand, two hundred and thirty at the end.

Then, from **1,250** count on in **10s** to the next **multiple of 100s**, 1,260, 1,270, 1,280, 1,290, **1,300** equal to **fifty**.

Next, from **1,300** count on in **100s** to the next **multiple of 1,000s**, 1,400, 1,500, 1,600, 1,700, 1,800, 1,900, **2,000** equal to **seven hundred**.

Then, from 2,000 count on in 1,000s to the next multiple of 1,000s, 3,000 equal to one thousand.

Next, from 3,000 count on in 100s to the multiple of 100s before 3,230, 3,100, 3,200 equal to two hundred.

Then, from 3,200 count on in 10s on to 3,230, 3,210, 3,220, 3230, equal to thirty.

Next, add from largest to smallest the amounts that were counted on, 1,000 and 700 and 200 and 50 and 30.

Finally, the missing number is 1,980.

#### Column Addition

# **Test Questions**

$$2)$$
 \_\_\_ +  $2,230$  =  $4,700$ 

$$6)$$
  $420 + = 2,600$ 

# Bonds to 1,000

1) 
$$150 + ? = 1,000$$

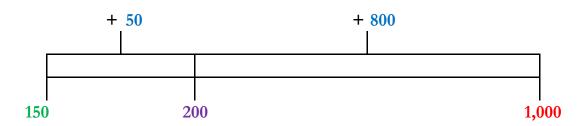
#### Word Problem

A Charity Shop has raised one hundred and fifty pounds in donations.

The **total amount** to be raised is **one thousand** pounds.

How much more money is needed to be raised?

#### Number Line



#### **Strategy Applied**

Number bonds to 1,000, means two or more numbers added together that make the number 1,000.

First, draw a number line and write one hundred and fifty at the start and one thousand at the end.

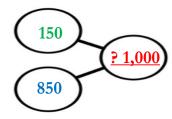
Then, from **150** count on in **10s** to the next **multiple of 100s**, 160, 170, 180, 190, **200** equal to **fifty**.

Next, from **200** count on in **100s** up to **one thousand**, 300, 400, 500, 600, 700, 800, 900, **1,000** equal to **800**.

Then, add from **largest to smallest** the amounts counted on **800** and **50**, equal to **850**.

Finally, the value of the missing number is eight hundred and fifty.

#### Part Whole Model



# **Test Questions**

$$5)$$
  $=$   $190p$  =  $1000p$ 

6) 
$$+ 270p = 1000p$$

7) 
$$+ £300 = £1,000$$

8) + 
$$£500 = £1,000$$

$$9) + 100 = 1,000$$

$$10) + 720 = 1,000$$

$$11) + 250 = 1,000$$

$$12)_{\underline{\phantom{0}}} + 570 = 1,000$$

$$13) + 480 = 1,000$$

#### **Bar Model**

150	<u>? 850</u>
	1,000

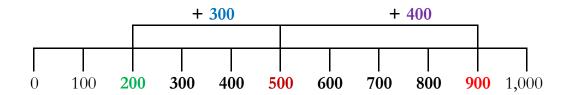
# Multiple Numbers

#### Word Problem

Three children raise money for a Homeless Charity. **Child A** raised £200, **Child B** raised £300 and **Child C** raised £400.

What is the **total amount** of money raised by all three children?

#### Number Line



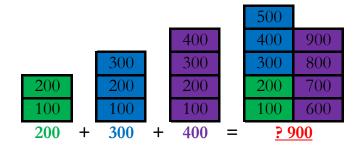
#### **Strategy Applied**

First, find and touch the number two hundred on the number line.

Then, **count forwards 300** more in **multiples of 100s**, 300, 400, **500** aloud in number order, whilst touching the numbers on the number line. Next, the number counted on to should be **five hundred**.

Then, **count forwards 400** more in multiples of **100s**, 600, 700, 800, **900** aloud in number order, whilst touching the numbers on the number line. Next, the number counted on to should be **nine hundred**. Finally, **200** plus **300** plus **400** equals **900**.

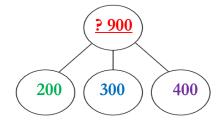
#### **Concrete Object**



#### Column Addition

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#### Part Whole Model



## **Test Questions**

7) 
$$100p + 500p + 200p =$$

8) 
$$\pounds 400 + \pounds 500 + \pounds 900 =$$

9) 
$$200cm + 400cm + 300cm =$$

10) 
$$400m + 500m + 600m = ____$$

$$11) = 700 + 900 + 600$$

$$12) = 1,500 + 1,500 + 1,500$$

$$13) = 900 + 900 + 700$$

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#### **Bar Model**

200	300	400		
<u>? 900</u>				

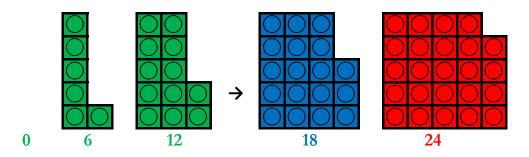
# Multiples of 6, 7, 9, 25, 100

In the **number pattern** below, find the next two missing **terms**.

#### Word Problem

Lee uses objects to make the **number pattern** of **zero**, **six** and **twelve**. What will be the next two **terms** in the number pattern?

#### **Concrete Object**



# **Strategy Applied**

Work out the **number pattern**, by finding out the **difference between** the **three** numbers.

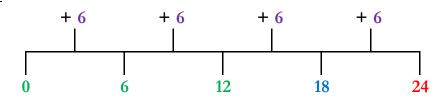
The difference between each of the **three** numbers is known as the **rule**. First, **count forwards** from **zero** to **six** equalling **six**, the rule is **+6**. Then, count forwards from **six** to **twelve** equalling **six**, the rule is **+6**. The rule is **+6** (**count on six**) to each of the numbers in the number pattern.

Continue this number pattern to find the next two missing numbers. Next, find **twelve** on the number line and count on **six** more, equal to **eighteen**.

Then, find **eighteen** on the number line and count on **six** more, equal to **twenty four**.

Finally, the next two missing terms in the number pattern are **eighteen** and **twenty four**.

# **Metric Ruler**



# **Test Questions**

- 1) 0, 6, 12, \_\_\_,
- 2) 24, 30, 36, \_\_\_,
- 3) 40, 46, 52, \_\_\_,
- 4) 0, 7, 14, \_\_\_,
- 5) 28, 35, 42, \_\_\_,
- 6) 50, 57, 64, \_\_\_,
- 7) 0, 9, 18, \_\_,
- 8) 36, 45, 54, \_\_\_,
- 9) 10, 19, 28, ,
- 10) 0, 25, 50, \_\_\_,
- 11) 20, 45, 70, \_\_\_,
- 12) 100, 125, 150, \_\_\_,
- 13) 15, 115, 215, \_\_\_,
- 14) 383, 483, 583, \_\_\_,

# **Decimals**

#### Word Problem

Mr. Ben and Dr. Barrie are playing guess my number.

The number is one point eight more than two point one.

# **Partitioning**

## **Strategy Applied**

**Partition** both numbers into **1s**, **10ths** and add together their relative digit values.

$$2.1 = 2.0 + 0.1$$
 and  $1.8 = 1.0 + 0.8$ .

First, add the 1s place values of two and one, which is equal to three.

Then, add the **10ths** place values of **zero point one** and **zero point eight**, which is equal to **zero point nine**.

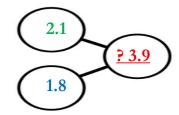
Next, use column addition to add the values of 3.0 + 0.9 = 3.9.

Finally, **2.1** plus **1.8** is equal to **3.9**.

#### **Decimal Number Grid**

	2.1								
3.0	3.1 -	<b>→</b> 3.2	3.3	3.4	3.5	3.6	3.7	3.8 -	3.9

# Part Whole Model



# **Test Questions**

6) 
$$4.7 + 2.1 =$$

10) 
$$3.6 + 3.2 =$$

$$11) = 5.4 + 2.2$$

$$12) = 6.7 + 3.3$$

$$13) = 5.5 + 1.7$$

$$14) = 7.2 + 1.9$$

# Bar Model

2.1	1.8
	<u>? 3.9</u>

# Column Addition

#### Step 1

# Step 2

# Step 3

#### Strategy Applied

#### Step 1

First, in the 1s column add altogether, 5 + 6, equals 11 ones (10 + 1). Write 1 in the total value of the 1s column.

Exchange/Regroup the 10 ones into 1 ten the from the 1s column to the 10s column and write 1 ten below the total value line of the 10s column. Then, in the 10s column add altogether, 3 + 4 + 1, equals 8 tens (80). Write 8 in the total value of the 10s column.

#### Step 2

Next, in the **100s** column add **altogether**, 8 + 2, equals 10 **hundreds** (1,000 + 0).

Write 0 in the total value of the 100s columns.

Exchange/Regroup the 10 hundreds into 1 thousand from the 100s column to the 1,000s column and write 1 thousand below the total value line of the 1,000s column.

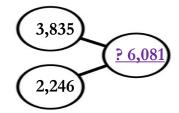
## Step 3

Finally, in the **1,000s** column add **altogether**, 3 + 2 + 1, equals 6 thousands (6,000).

Write 6 in the total value of the 1,000s column.

Total value is 6,081.

#### Part Whole Model



#### **Bar Model**

3,835	2,246		
? 6,081			

# **Test Questions**

# **Column Addition with Decimals**

1) 
$$4 \ 8 \ . \ 5 \ 3 \ + \ 2 \ 5 \ . \ 7 \ 1 = ?$$

# **Strategy Applied**

#### Step 1

First, in the **100ths** column add **altogether**, 3 + 1, equals 4 **hundredths** (0.04).

## Step 2

Then, in the **10ths** column add **altogether**, 5 + 7, equals 12 **tenths** (1 + 0.2).

Write 2 in the total value of the 10ths column.

Exchange/Regroup the 10 tenths into 1 one from the 10ths column to the 1s column and write 1 one below the total value line of the 1s column.

#### Step 3

Next, in the 1s column add altogether, 8 + 5 + 1, equals 14 ones (10 + 4). Write 4 in the total value of the 1s column.

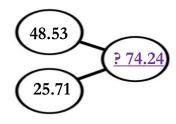
Exchange/Regroup the 10 ones into 1 ten from the 1s column to the 10s column write 1 ten below the total value line of the 10s column.

## Step 4

Finally, in the **10s** column add **altogether**, 4 + 2 + 1, equals 7 **tens** (70). Write 7 in the **total value** of the **1s** column.

Total Value is 74.24.

# Part Whole Model



# **Bar Model**

48.53	25.71			
<u>? 74.24</u>				

#### **Test Questions**

Page 20

# Find the Missing Number

1) 
$$7942cm + 379cm = ? cm + 7,021cm$$

#### **Strategy Applied**

Step 1

First, add up the **known number sentence**, which is **7942cm** + **379cm**.

Then, in the 1s column add altogether, 2 + 9, equals 11 ones (10 + 1). Write 1 in the total value of the 1s column.

Exchange/Regroup the 10 ones into 1 ten from the 1s column to the 10s column and write 1 ten below the total value line of the 10s column.

Next, in the 10s column add altogether, 4 + 7 + 1, equals 12 tens (100 + 20).

Write 2 in the total value of the 10s column.

Exchange/Regroup the 10 tens into 1 hundred from the 10s column to the 100s column and write 1 hundred below the total value line of the 100s column.

Then, in the **100s** column add **altogether**, 9 + 3 + 1, equals 13 hundreds (1000 + 300).

Write 3 in the total value of the 100s column.

Exchange/Regroup the 10 hundreds into 1 thousand from the 100s column to the 1,000s column and write 1 thousand below the total value line of the 1,000s column.

In the 1,000s column add altogether, 7 + 1, equals 8 thousands (800).

Finally write 8 in the total value of the 1,000s column.

Total value is 8,321.

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#### Step 2

New known fact

$$8321cm = ? cm + 7,021cm$$

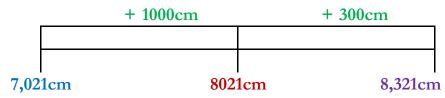
The value of the **10s** and **1s** in **8,321** and **7,021** are the same, **21**.

First, **count on** in **1,000s**, **7,021cm** on to **8,021cm**, equal to **1,000cm**.

Then, count on in 100s, 8,021cm up to 8,321cm, equal to 300cm.

Finally, add the amounts counted on 1,000cm and 300cm, equals 1,300cm.

#### Number Line



#### **Test Questions**

1) 
$$7,942$$
cm +  $379$ cm = cm +  $7,021$ cm

3) 
$$£2.45 + £1.75 =$$

4) 
$$£8.56 + 208 \text{ pence} + 75 \text{ pence} =$$

7) 
$$3 \text{ litres} = __m \text{ml} + 1257 \text{ ml}$$
 12)  $63 + 9 + 9 = __m$ 

$$12) 63 + 9 + 9 = \underline{\hspace{1cm}}$$

$$13)$$
  $250$  +  $25$  +  $25$  =

# <u>1,000 Less</u>

#### Word Problem

A road is one thousand, two hundred and eighty metres long.

Diane cycles one thousand metres along the road.

How much **further** to the end of the road?

#### **Partitioning**

#### **Column Subtraction**

#### **Strategy Applied**

Partition both numbers into 1,000s, 10s, 10s, 1s and subtract their relative digit values.

1,280 = 1,000 + 200 + 80 + 0 and 1,000 = 1,000 + 0 + 0 + 0.

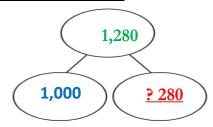
First, subtract the **1,000s** digit values of **one thousand** and **one thousand**, which is equal to **zero**.

Then, subtract the **100s** digit values of **two hundred** and **zero**, which is equal to **two hundred**.

Next, subtract the **10s** digit values of **eighty** and **zero**, which is equal to **eighty**.

Then, subtract the **1s** digit values of **zero** and **zero**, which is equal to **zero**. Then, use column addition to add the values of 200 + 80 + 0 + 0 = 280. Finally, **1,280** minus **1,000** is equal to **280**.

#### Part Whole Model



#### **Test Questions**

$$12) = 4,784 - 1,000$$

#### Bar Model

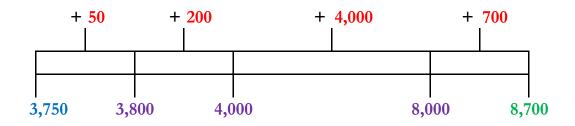
1,280	
1,000	<u>? 280</u>

# More Than 1,000

#### Word Problem

My parents are thinking of buying a new car costing **eight thousand**, **seven hundred** pounds. They decide to buy a car that is **three thousand**, **seven hundred and fifty** pounds **cheaper**. What is the cost of the car?

#### Number Line



#### **Strategy Applied**

Use the **inverse** of subtraction, which is addition and **count on** from the **smallest** number to the **largest** number.

Use a ruler or number grid to help when counting on.

First, draw a number line and write three thousand, seven hundred and fifty at the start and eight thousand, seven hundred at the end. Then, from 3,750 count on in 10s to the next multiple of 100s, 3,760,

3,770, 3,780, 3,790, **3,800** equal to **fifty**.

Next, from 3,800 count on in 100s to the next multiple of 1,000s, 3,900, 4,000 equal to two hundred.

Then, from **4,000** count on in **1,000s** to the **multiple of 1,000s** before **8,700**, 5,000, 6,000, 7,000, **8,000** equal to **four thousand**.

Next, from **8,000** count on in **100s** to **8,700**, 8,100, 8,200, 8,300, 8,400, 8,500, 8,600, **8,700** equal to seven hundred.

Next, add the amounts counted on from **largest** to **smallest**, **4,000** and **700** and **200** and **50**.

Finally, the missing number is **4,950**.

#### Column Addition

#### **Test Questions**

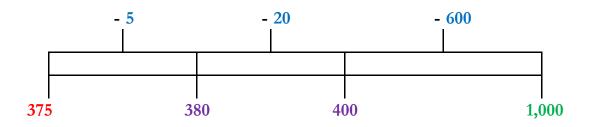
# **Bonds to 1,000**

#### Word Problem

Rafique's missing number is the **difference** between **one thousand** and **three hundred and seventy five**.

What is his missing number?

#### **Number Line**



#### **Strategy Applied**

Number bonds to 1,000, means two or more numbers added together that make the number 1,000.

Use a ruler or number grid to help when counting on.

First, draw a number line and write three hundred and seventy five. at the start and one thousand at the end.

Then, from **1,000** count back in **100s** to the **multiple of 100s** before **375**, 900, 800, 700, 600, 500, **400** equal to **six hundred**.

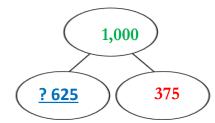
Next, from 400 count back in 10s to the multiple of 10s before 375, 390, 380 equal to twenty.

Then, from **380** count back in **1s** back to **375**, 379, 378, 377, 376, **375** equal to **five**.

Next, add the amounts counted on from largest to smallest, 600 and 20 and 5 equal to 625.

Finally, the missing number is 625.

#### Part Whole Model



#### **Test Questions**

#### **Bar Model**

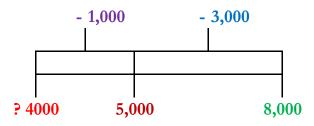
1,000	
<u>? 625</u>	375

# Multiple Numbers

#### Word Problem

**Eight thousand** fans are seated at the Olympic Stadium. At **6pm three thousand** fans leave the stadium. It's **7.30pm** and **one thousand** more fans leave. How many fans are **left** in the stadium?

#### Number Line



#### **Strategy Applied**

First, draw a number line and write a ? at the start and eight thousand at the end.

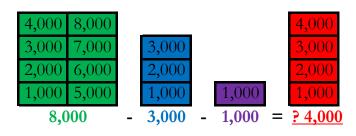
First, find and touch the number **eight thousand** on the number line. Then, **count backwards 3,000** less in **multiples of 1,000s**, 7,000, 6,000, **5,000** equal to **5,000**.

Next, the number counted back to should be **five thousand**.

Then, count backwards 1,000 less in multiples of 1,000s, 4,000 equal to 4,000.

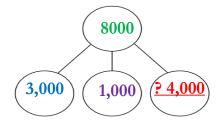
Next, the number counted back to should be **four thousand**. Finally, **8,000** subtract **3,000** subtract **1,000** equals **4,000**.

## Concrete Object



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#### Part Whole Model



#### **Test Questions**

$$12) = 4,500 - 1,500 - 150$$

$$14) = 6,000 - 200 - 100$$

#### **Bar Model**

8,000						
3,000	1,000	<u>? 4,000</u>				

# Multiples of 6, 7, 9, 25, 100

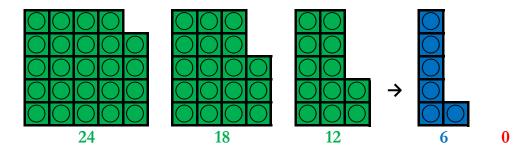
In the **number pattern** below, find the next two missing **terms**.

#### Word Problem

David uses cubes to make the **number pattern** of **twenty four**, **eighteen** and **twelve**.

What are the next two missing terms?

#### Concrete Object



#### **Strategy Applied**

Work out the **number pattern**, by finding out the **difference between** the **three** numbers.

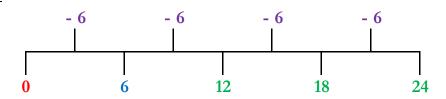
The difference between each of the **three** numbers is known as the **rule**. First, **count backwards** from **twenty four** to **eighteen** equalling **six**, the rule is **-6**.

Then, count backwards from **eighteen** to **twelve** equalling **six**, the rule is **-6**.

The rule is **-6** (**count back six**) each number in the number pattern. Continue this number pattern to find the next two missing numbers. Next, find **twelve** on the number line and count back **six less**, equal to **six**.

Then, find six on the number line and count back six less, equal to zero. Finally, the next two missing terms in the number pattern are six and zero.

## Metric Ruler



- 1) 24, 18, 12, \_\_\_,
- 2) 39, 33, 27, \_\_\_\_,
- 3) 51, 45, 39, \_\_\_,
- 4) 52, 45, 38, \_\_\_,
- 5) 64, 57, 50, \_\_\_,
- 6) 76, 69, 62, \_\_\_\_,
- 7) 101, 92, 83, \_\_,
- 8) 210, 201, 192, \_\_\_,
- 9) 305, 296, 287, \_\_\_,
- 10) 420, 411, 402, ,
- 11) 725, 700, 675, <u>,</u>
- 12) 950, 925, 900, \_\_\_,
- 13) 1,200, 1,100 1,000 \_\_\_,
- 14) 2,700, 2,600 2,500 \_\_\_,

## **Decimals**

#### Word Problem

In the Arctic, the temperature was **two point one** degrees above freezing on Saturday and **one point eight** degrees above freezing on Sunday. What was the **difference** in temperatures?

#### Number Grid

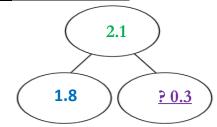
0.0	0.1	0.2	0.3	- 0.4	0.5	0.6	0.7	0.8	- 0.9
1.0	- 1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9
2.0	2.1	2.2	2.3	2.4	2.5	2.6	2.7	2.8	2.9

#### **Strategy Applied**

**Partition 1.8** into **1.0** + **0.8** and subtract each partitioned value from **2.1**. First, find and touch the number **two point one** on a decimal number grid. Then, **count upwards one square** which is **1.0** less aloud in number order, whilst touching the numbers on the number grid, equal to **one point one**. Next, **count backwards 0.8** less aloud in number order, whilst touching the numbers on the number grid, 1.0, 0.9, 0.8, 0.7, 0.6, 0.5, 0.4, **0.3** equal to **zero point three**.

Finally, the value of the missing number is zero point three.

## Part Whole Model



## **Test Questions**

- 1) 2.1 1.8 = \_\_\_\_
- 2) 2.5 1.3 =
- 3) 6.3 2.6 =
- 4) 7.5 1.4 = \_\_\_\_
- 5) 6.2 1.7 = \_\_\_\_
- 6) 4.7 2.1 =
- 7) 4.4 3.7 =
- 8) 6.1 3.9 =
- 9) 8.1 1.9 = \_\_\_\_
- 10) 3.6 3.2 = \_\_\_\_
- 11) = 5.4 2.2
- 12) = 6.7 3.3
- 13) = 5.5 1.7
- 14) = 7.2 1.9

## Bar Model

2.1	
1.8	<u>? 0.3</u>

## Column Subtraction

Step 1	Step 2	Step 3	Step 4
	5	5	E
		_	3
3 6 5 7	3 6 <sup>1</sup> 5 7	3 6 15 7	3 6 <sup>1</sup> 5 7
-2 4 6 5	- 2 4 6 5	- 2 4 6 5	- 2 4 6 5
2	9 2	1 9 2	1, 1 9 2

#### **Strategy Applied**

#### Step 1

In the **1s** column, **7** subtract 6, equals 2 **ones** (2).

Write 2 in the total value of the 1s column.

#### Step 2

In the **10s** column, 5 subtract 6, you cannot do as 5 is a **lower value** than 6. **Exchange/Regroup 1 hundred** into **10 tens** from the **100s** column to the **10s** column.

Cross out the 6 tens and write 5 tens above, then write the exchanged/regrouped 1 ten next to the 5 ones to make 15 ones.

In the 10s column, 15 subtract 6, equals 9 tens (90).

Write 9 in the total value of the 10s column.

## Step 3

In the 100s column, 5 subtract 4, equals 1 hundred (100).

Write 1 in the total value of the 100s column.

## Step 4

In the **1,000s** column, 3 subtract 2, equals 1 **thousand** (**1,000**).

Write 1 in the total value of the 1,000s column.

Total value is 1,192.

## Column Subtraction

Step 1	Step 2	Step 3	Step 3
2	5 2	5 2	5 2
3 6 <b>3 1</b> 5	3 6 13 15	3 6 13 15	3 6 13 15
-2 4 4 6	- 2 4 4 6	- 2 4 4 6	- 2 4 4 6
9	8 9	1 8 9	1, 1 8 9

#### **Strategy Applied**

#### Step 1

In the 1s column, 5 subtract 6, you cannot do as 5 is a lower value than 6. Exchange/Regroup 1 ten into 10 ones from the 10s column to the 1s column.

Cross out the 3 tens and write 2 tens above, then write the exchanged/regrouped 1 ten next to the 5 ones to make 15 ones.

In the **1s** column, **1**5 subtract 6, equals 9 **ones** (9).

Write 9 in the total value of the 1s column.

#### Step 2

In the 10s column, 2 subtract 4, you cannot do as 2 is a lower value than 4. Exchange/Regroup 1 hundred into 10 tens from the 10s column to the 10s column.

Cross out the 6 hundreds and write 5 tens above, then write the exchanged/regrouped 1 hundred next to the 2 tens to make 12 tens.

In the 10s column, 12 subtract 4, equals 8 tens (80).

Write 8 in the total value of the 10s column.

#### Step 3

In the 100s column, 5 subtract 4, equals 1 hundred (100).

Write 1 in the total value of the 100s column.

## Step 4

In the 1,000s column, 3 subtract 2, equals 1 thousand (1,000).

Write 1 in the total value of the 1,000s column.

Total value is 1,549.

# **Column Subtraction**

#### **Strategy Applied**

#### Step 1

In the **1s** column, 0 subtract 8, you cannot do as 0 is a **lower value** than 8. From the **10s** column, **regroup** 1 **ten** from the 0 **tens**, you cannot do this as the value of the **tens** is zero.

From the **100s** column, **regroup** 1 **hundred** from the 0 **tens**, you cannot do this as the value of the **hundreds** is zero.

Instead, exchange/regroup 1 thousand into 10 hundreds from the 1,000s column to the 10s column.

Cross out the 3 thousands and write 2 thousands above, then write the exchanged/regrouped 1 thousand next to the 0 hundreds to make 10 hundreds.

## Step 2

Exchange/Regroup 1 hundred into 10 tens from the 100s column to the 10s column.

Cross out the 10 hundreds and write 9 hundreds above, then write the exchanged/regrouped 1 hundred next to the 0 tens to make 10 tens.

#### Step 3

Exchange/Regroup 1 ten into 10 ones from the 10s column to the 1s column.

Cross out the 10 tens and write 9 tens above, then write the exchanged/regrouped 1 ten next to the 0 ones to make 10 ones.

## Step 4

In the 1s column, 10 subtract 8, equals 2 ones (2).

Write 2 in the total value of the 1s column.

In the **10s** column, **9** subtract 4, equals 5 **tens** (50).

Write 5 in the total value of the 10s column.

In the 100s column, 9 subtract 4, equals 5 hundreds (500).

Write 5 in the total value of the 100s column.

In the **1,000s** column, **2** subtract 2, equals 0 thousands (0).

Write 0 in the total value of the 1,000s column.

Total value is 552.

# **Column Subtraction with Decimals**

1) 7 9 . 5 + 2 4 . 6 = 
$$?$$

#### Word Problem

The perimeter of a farm is twenty four point six kilometres fewer than seventy nine point five kilometres.

What is the perimeter of the farm?

## Step 1

## Step 2

## Step 3

## **Strategy Applied**

#### Step 1

In the **10ths** column, 5 subtract 6, you cannot do as 5 is a **lower value** than 6.

Exchange/Regroup 1 one into 10 tenths from the 1s column to the 10ths column.

Cross out the 9 ones and write 8 ones above, then write the exchanged/regrouped 1 one next to the 5 tenths to make 15 tenths.

## Step 2

In the **10ths** column, **1**5 subtract 6, equals 9 **tenths** (**0.9**).

Write 9 in the total value of the 10ths column.

## Step 3

In the 1s column, 8 subtract 4, equals 4 ones (4).

Write 4 in the total value of the 1s column.

In the **10s** column, 7 subtract 2, equals 5 tens (50).

Write 5 in the total value of the 10s column.

Total value is 54.9.

#### Part Whole Model



#### **Bar Model**

79.5						
24.6	<u>? 54.9</u>					

# Find the Missing Number

#### Word Problem

Two thousand fewer than the missing number is equal to the total value of the first number sentence.

Step 1
 Step 2

 
$$8, 7000$$
 $7, 7000$ 
 $-\frac{1}{7}, 7000$ 
 $\frac{7}{9}, 7000$ 

#### **Strategy Applied**

#### Step 1

First, subtract the known number sentence, which is 8,700 - 1,000.

Then, partition eight thousand, seven hundred into its digit values. 8,000 + 700 + 0 + 0.

From the digit value of the **1,000s place value**, **eight thousand**, subtract the **one thousand**. **8,000 - 1,000 = 7,000** 

The digit value of the **100s**, **10s** and **1s** in **8,700** will remain the same as 700 + 0 + 0.

Next, the new partitioned values are 7,000 + 700 + 0 + 0 equal to 7,700. Finally, 8,700 subtract 1,000 is equal to 7,700.

## Step 2

Now we know 7,700 = ? - 2,000

Use the **inverse** to calculate the missing number 7,700 + 2,000 = ?Then, **partition seven thousand, seven hundred** into its **digit values**. 7,000 + 700 + 0 + 0. From the digit value of the 1,000s place value, seven thousand add the two thousand. 7,000 + 2,000 = 9,000

The digit value of the **100s**, **10s** and **1s** in **7,700** will remain the same as 700 + 0 + 0.

Next, the new partitioned values are 9,000 + 700 + 0 + 0, equal to 9,700. Finally, the **value** of the missing number is equal to 9,700.

4) 
$$£3.42 - £1.72 =$$

5) 
$$450 + \underline{\phantom{0}} - 226 = 1,000$$

# **Step Counting**

1) 
$$= 4 \times 12$$

#### Word Problem

There are **four** fish in one jar. How many fish are there in **twelve** jars?

#### **Number Line**

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41
42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62

#### **Strategy Applied**

The twelve represents the value in each group, the multiplicand. The four represents how many groups there are, the multiplier. The ? represents the total value of four groups of twelve, the product. For step counting each lot of twelve is added on four times up to ?, expressing the number value as it is counted on.

First, find and touch the number **zero** on a number line.

Then, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **twelve**.

Next, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **twenty four**. Then, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **thirty six**.

Next, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **forty eight**.

Finally, **twelve** lots of **four** equals **forty eight**.

# **Step Counting**

## 12 → 24 → 36 → 48 • • • •

# 12 12 12 12

Bar Model

4) 
$$_{--}$$
 = 5 x 5

$$5)$$
 \_\_\_ =  $7 \times 11$ 

$$6) = 4 \times 4$$

$$7) = 12 \times 8$$

$$8) = 6 \times 6$$

9) = 
$$9 \times 3$$

$$10)_{\underline{\phantom{0}}} = 8 \times 6$$

11) = 
$$9 \times 9$$

$$13) = 8 \times 3$$

$$14)_{\underline{}} = 7 \times 6$$

# **Multiple Numbers**

1) 
$$2 \times 5 \times 4 = ?$$

#### Word Problem

Two pencils are placed in each pot.

There are **five** pots in one row.

What is the **total** number of pencils in **four** rows?

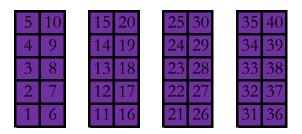
## Step 1





# Step 2





## **Strategy Applied**

The three numbers can be multiplied in any order.

Out of the **three** numbers, multiply two of them together first and the **product** (answer) will then be multiplied by the remaining number.

## Step 1

Use step counting to multiply two by five, equal to ten.

## Step 2

Use step counting to multiply ten by four, equal to forty.

The total value of the product is forty.

- 1) 2 x 5 x 4 = \_\_\_\_
- 2) 5 x 3 x 5 = \_\_\_\_
- 3) 2 x 3 x 5 = \_\_\_\_
- 4) 5 x 6 x 4 = \_\_\_\_
- 5) 2 x 3 x 8 = \_\_\_\_
- 6)  $7 \times 7 \times 3 =$
- 7) 2 x 3 x 7 = \_\_\_\_
- 8) 8 x 3 x 4 = \_\_\_\_
- 9) 3 x 4 x 6 = \_\_\_\_
- 10) 3 x 4 x 7 =  $\underline{\phantom{a}}$
- 11) =  $20 \times 3 \times 7$
- 12)  $= 80 \times 3 \times 4$
- 13)  $= 30 \times 4 \times 60$
- $14) = 30 \times 40 \times 70$

## x10 and x100

1) 
$$26 \times 100 = ?$$

#### Word Problem

A race from London to Brighton is **one hundred** miles long. Only **twenty six** of the participants complete the race. The collective number of miles ridden by them all is **how much?** 

#### Place Value Grid

<u>Thousands</u> <u>1,000s</u>	<u>Hundreds</u> <u>100s</u>	<u>Tens</u> <u>10s</u>	<u>Ones</u> <u>1s</u>
		2	6
2	6	0	0

#### **Strategy Applied**

Multiplying any number by **one hundred**, means that number will become **one hundred times as big**.

Each **digit** in the number will move **two column place values** to the **left**. First, write the number **twenty six** on a **place value grid**, in the **1s** and **10s** column.

Then, in the **10s** column multiply the digit **two** by **one hundred** by moving it **two column place values** to the **left** and write **two** in the **1,000s** column.

Next, in the 1s column multiply the digit six by one hundred by moving it two column place values to the left and write six in the 10s column. Then, the 10s and 1s column cannot be left blank as they still have a value, write zero, a place holder in both columns.

Finally, 26 multiplied by 100 is equal to 2,600.

- 1) 26 x 100 = \_\_\_
- 2)  $39 \times 10 =$
- 3) 41 x 100 = \_\_\_
- 4)  $58 \times 10 =$
- 5)  $63 \times 100 =$
- 6)  $72 \times 10 =$
- 7)  $80 \times 100 =$
- 8) 94  $\times$  10 = \_\_\_\_
- 9)  $75 \times 100 =$
- 10) 53  $\times$  10 = \_\_\_\_
- 11)  $91 \times 100 =$
- 12)  $82 \times 10 =$
- 13) 64 x 100 = \_\_\_
- 14) 55 x 10 = \_\_\_

# **Short Multiplication**

1) 2, 1 3 5 
$$\times$$
 4 = ?

#### Word Problem

Over four years, two thousand, one hundred and thirty five pounds is saved each year.

How much is saved in total?

## **Strategy Applied**

#### Step 1

In the 1s column, multiply 5 by 4, equals 20 ones (20 + 0).

Write 0 in the total value of the 1s column.

Exchange/Regroup the 20 ones into 2 tens from the 1s column to the 10s column and write 2 tens below the total value line of the 10s column.

#### Step 2

In the **10s** column, multiply (30) **3** by **4**, equals 12 tens (100 + 20). Add the exchanged/regrouped 2 tens (20) below, equals 14 tens (100 + 40).

Write 4 in the total value of the 10s column.

Exchange/Regroup the 10 tens into 1 hundred from the 10s column to the 100s column and write 1 below the total value line of the 100s column.

## Step 3

In the **100s** column, multiply (100) **1** by **4**, equals 4 **hundreds** (**400**). Add the **exchanged/regrouped 1 hundred** (100) below, equals 5 **hundreds** (**500**).

Write 5 in the total value of the 100s column.

## Step 4

In the **1,000s** column, multiply (2,000) **2** by **4**, equals **8 hundreds** (**800**). Write **8** in the **total value** of the **1,000s** column. **Total value** is **8,540**.

#### **Bar Model**

2,135	2,135	2,135	2,135			
8,540						

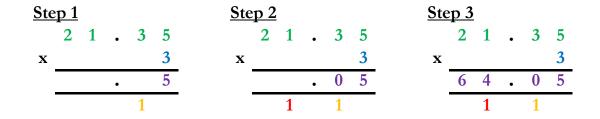
1) 2 8	2) 6 4	3) 2 1 4	4) 2 1 3 5
x 4	x 8	x 5	x 4
5) 4 7	•	7) 3 7 5	8) 8 2 5 7
x 9		x 3	x 5
9) 4 3	10) 6 3	11) 1 7 6	12) 7 3 4 0
x 9	x 3	x 4	x 9

# **Short Multiplication with Decimals**

1) 2 1 . 3 5 
$$x$$
 3 = ?

#### Word Problem

One bag of cement weighs **twenty one point three five** kilograms. What is the weight of **three** bags?



## **Strategy Applied**

#### Step 1

In the 100ths column, multiply 5 by 3, equals 15 hundredths (0.10 + 0.05).

Write 5 in the total value of the 100ths column.

Exchange/Regroup the 10 hundredths into 1 tenth from the 10ths column to the 10ths column and write 1 tenth below the total value line of the 10ths column.

## Step 2

In the **10ths** column, multiply **3** by **3**, equals **9 ones** (**0.09**). Add the **exchanged/regrouped 1 tenth** below, equals 10 **tenths** (**1.0** + **0.0**).

Write 0 in the total value of the 10ths column.

Exchange/Regroup the 10 tenths into 1 one from the 10ths column to the 1s column and write 1 one below the total value line of the 1s column.

#### Step 3

In the 1s column, multiply 1 by 3, equals 3 ones (3).

Add the **exchanged/regrouped 1** one below, equals 4 **ones** (4).

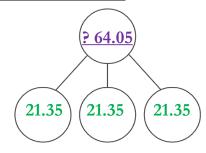
Write 4 in the total value of the 1s column.

In the **10s** column, multiply **2** by **3**, equals 6 **tens** (**6**).

Write 6 in the total value of the 10s column.

Total value is 64.05.

#### Part Whole Model



## **Bar Model**

21.35	21.35	21.35				
	? 64.05					

# Find the Missing Number

1) 
$$34 \times 5 =$$
  $30$ 

#### Word Problem

**Five** packets of **thirty four** sunflower seeds are planted in **Garden A**. **Garden B** plants the same amount of seeds.

#### Step 1

#### **Strategy Applied**

#### Step 1

Calculate the **known number sentence 34** x **5**, using **partitioning**.

There are five lots of thirty fours,

**Partition** the number **thirty four** into its digit values **30** + **4**, multiplicand.

Multiply each digit value by five, the multiplier.

First, multiply thirty by five, equal to one hundred and fifty.

Then, multiply **four** by **five**, equal to **twenty**.

Finally, add together one hundred and fifty and twenty, equal to one hundred and seventy.

## Step 2

## Step 2

New **known fact** 170 = ? - 30 or ? - 30 = 170

Use the **inverse** of subtraction, which is addition and add together,

$$170 + 30 = ?$$

Partition one hundred and seventy into its digit values 100 + 70 + 0.

As only thirty is to be added, the digit value of the **10s** column will change in the number **170**, which is **70**.

**70** add **30** is equal to **100**.

The digit value of the **100s** and **10s** in **170** will remain the same as 100 + 0.

Next, the new partitioned values are 100 + 100 + 0.

Finally, 100 + 70 + 0 add 30 is equal to 200.

1) 
$$34 \times 5 = -30$$

8) 9 x 4 x 2 = 
$$\_$$

2) 
$$3 \times 8 = \times 4$$

9) 
$$3 \times 8 = \times 4$$

3) 
$$7 \times 3 \times 0 =$$

10) 4 x 8 x 8 = 
$$\underline{\phantom{a}}$$

4) 4 x 6 x 10 = 
$$\underline{\phantom{a}}$$

11) 25 x 3 = 
$$\underline{\hspace{1cm}}$$
 x 5

5) 
$$4 \times 3 \times 6 =$$

12) 8 x 3 x 
$$0 =$$

6) 
$$3 \times 7 \times 7 =$$

13) 
$$6 \times 8 = _{x} \times 4$$

7) 
$$24 \times 5 = \times 10$$

14) 
$$345 \times 8 = 3450 -$$

## **Inverse of Division**

1) 
$$36 \div ? = 12$$

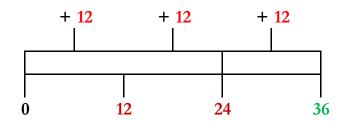
#### Word Problem

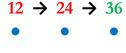
A number of children share **thirty six** pounds equally between them, they each receive **twelve** pounds.

How many children are there?









#### **Strategy Applied**

The thirty six represents the total value, the dividend.

The missing number represents how many groups of thirty six, the divisor.

The twelve represents the value in each equal group, the quotient.

Use the inverse of division is multiplication,

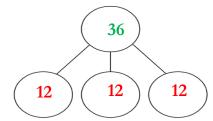
12 x ? = 36

Apply step counting to calculate the missing number, the divisor, by counting on lots of twelves on to thirty six.

First, find and touch the number zero on a number line.

Then, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **twelve**. Then, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **twenty four**. Then, **count forwards twelve** more aloud in number order, whilst touching the numbers on the number line, on to the number **thirty six**. Finally, **three** groups of **twelve** equals **thirty six**.

#### Part Whole Model



## **Test Questions**

$$6) \div 98 = 1$$

$$7)$$
  $\div$   $6 = 5$ 

9) 
$$\div$$
 11 = 10

## Bar Model

36						
12	12	12				

## ÷10 and ÷100

1) 
$$361 \div 100 = ?$$

#### **Word Problem**

A landmark building is **three hundred and sixty one** metres tall. Miniature replicas sold in the shops are **one hundred times as small**. How tall is a replica?

#### Place Value Grid

<u>1000s</u>	<u>100s</u>	<u>10s</u>	<u>1s</u>	•	<u>10ths</u>	<u>100ths</u>
	3	6	1	•		
			3	•	6	1

#### **Strategy Applied**

Dividing any number by **one hundred**, means that number will become **one hundred times as small**.

Each digit in the number moves two column place values to the right. First, write the number three hundred and sixty one on a Place Value Grid, in the 100s, 10s and 1s columns.

Then, in the **100s** column divide the digit **three** by **one hundred**, moving it **two column place values** to the **right** and write **three** in the **1s** column. Next, in the **10s** column divide the digit **six** by **one hundred**, moving it **two column place values** to the **right** and write **six** in the **10ths** column. Then, in the **1s** column divide the digit **one** by **one hundred**, moving it **two column place values** to the **right** and write **one** in the **100ths** column. Finally, **three hundred and sixty one** divided by **one hundred** is equal to **three point six one**.

## **Short Division**

#### Word Problem

Two cargo ships should have an **identical** number of crates of apple juice. Altogether they both hold **seven thousand**, **one hundred and thirty five** crates. How many crates does each ship hold?

## **Strategy Applied**

#### Step 1

How many **lots of 2** divide **exactly** in to 7? The answer is 3 (2 x 3 = 6), with a **remainder** of 1.

Write 3 on the line above the 7.

Cross out the 7 and regroup the remainder 1 to the next digit place value.

#### Step 2

How many **lots of 2** divide **exactly** in to 11? The answer is 5 (2 x 5 = 10), with a remainder of 1.

Write 5 on the line above the 11.

Regroup the remainder 1 to the next digit place value, 3, to become 13.

## Step 3

How many **lots of 2** divide **exactly** in to **13**? The answer is 6 (2 x 6 = 12), with a **remainder** of **1**.

Write 6 on the line above the 13.

**Regroup** the **remainder 1** to the next **digit place value, 5**, to become **15**.

## Step 4

How many **lots of 2** divide **exactly** in to **15**? The answer is 7 (2 x 7 = 14), with a **remainder** of 1.

Write 7 on the line above the 15.

## Step 5

There are no more **digits** in the number to be divided by **2**.

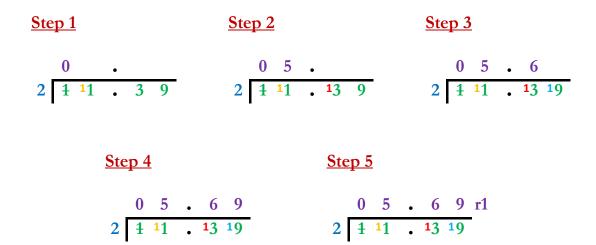
The **remainder** of 1, is written as **r1** on the line above.

Total value is 3,567 r1.

## **Short Division with Decimals**

#### Word Problem

Eleven point three nine pounds is to be shared equally between two kids. Can the amount of money be shared equally?



#### Strategy Applied

## Step 1

How many **lots of 2** divide **exactly** in to 1? The answer is  $0 (2 \times 0 = 0)$ , with **remainder 1**.

Write **0** on the line above the **1**.

Cross out the 1 and regroup the remainder 1 to the next digit place value, 1, to become 11.

#### Step 2

How many **lots of 2** divide **exactly** in to 11? The answer is 5 (2 x 5 = 10), with **remainder 1**.

Write 5 on the line above the 11 and write a **decimal point** next to it.

Regroup the remainder 1 to the next digit place value, 3, to become 13.

#### Step 3

How many lots of 2 divide exactly in to 13? The answer is 6 (2 x 6 = 12), with remainder 1.

Write 6 on the line above the 13.

**Regroup** the **remainder 1** to the next **digit place value, 9**, to become **19**.

## Step 4

How many **lots of 2** divide **exactly** in to **19?** The answer is **9** (2 x **9** = 18), with **remainder 1**.

Write 9 on the line above the 19.

## Step 5

There are no more **digits** in the number to be divided by **2**.

The **remainder 1**, is written as **r1** on the line above.

Total value is 5.68 r1.

# Find the Missing Number

1) 
$$40 \div 5 = ? \times 2$$

#### Word Problem

A basket contains **forty** strawberries. Noel has **five times as less**. Kavalli has the **same** amount as him, split into two tubs. How many strawberries in one tub?

$$\underbrace{\text{Step 1}}_{5} \quad 5 \rightarrow 10 \rightarrow 15 \rightarrow 20 \rightarrow 25 \rightarrow 30 \rightarrow 35 \rightarrow 40$$

## **Strategy Applied**

#### Step 1

Out of the two number sentences, calculate the number sentence with all the **known** numbers first,  $40 \div 5$ .

Apply **step counting**, the **inverse** of division, to calculate how many **lots of five** is equal to **forty**.

**Count forwards** saying the number names that are after the number.

First, find and touch the number five on a number line.

Then, count forwards aloud in number order, whilst touching the numbers on the number line, five more equal to six.

Next, keep repeating the action of counting on in **lots of fives** up to the number **forty** on a number line.

Finally, **eight lots of five** is equal to **forty**.



If  $40 \div 5 = 8$ , then 8 = ? x 2, as they are the same value.

Use step counting to calculate the missing number,  $2 \times ? = 8$ , by counting on in **lots of twos** up to **eight**.

Count forwards saying the number names that are after the number.

First, find and touch the number two on a number line.

Then, count forwards aloud in number order, whilst touching the numbers on the number line, two more equal to four.

Next, keep repeating the action of counting on in **lots of twos** up to the number **eight** on a number line.

Finally, **four lots of twos** is equal to **eight**, the missing number is **four**.

2) 
$$60 \div 5 = _{x} 6$$

3) 
$$7 \div 100 =$$

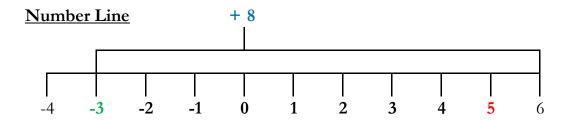
8) 
$$6 \div 10 =$$

10) 
$$72 \div = 9$$

## Add and Subtract Integers

#### Word Problem

The temperature on the last day of September in Scotland was minus three degrees. Yet England was eight degrees warmer on the same day. What was the temperature in England?



#### **Strategy Applied**

Positive numbers are counted on forwards on a horizontal number line and upwards on a vertical number line.

Negative numbers are counted on backwards on a horizontal number line and downwards on a vertical number line.

To **represent** positive and negative numbers on a number line, then mark **zero** half way (**mid-point**) on the line.

On a **horizontal** number line, all the numbers (**integers**) to the **right** of the **zero** will be **positive**.

On a **horizontal** number line, all the numbers (**integers**) to the **left** of the **zero** will be **negative**.

#### Step 1

Draw a **horizontal** number line and **half way** mark it with a **zero**. From the **zero**, count backwards in **multiples of 1s** to **minus three**. Mark the **minus three** on the number line.

#### Step 2

First, find and touch the number **minus three** on the number line. Then, count forwards **eight** more in **multiples of 1s** aloud in number order whilst touching the numbers on the number line, -2, -1, 0, 1, 2, 3, 4, 5 equal to **five**.

$$14) + 30 - 19 =$$

### To Nearest 10

#### Place Value Grid

<u>1000s</u>	<u>100s</u>	<u>10s</u>	<u>1s</u>	•	<u>10ths</u>	<u>100ths</u>
3	2	5	7	•		
3	2	6	0	•		

#### **Strategy Applied**

When rounding to the nearest 10s place value, the following will occur.

- 1. The **10s digit value** will remain the **same** (round down), if the digit in the **1s** column is a 0, 1, 2, 3, 4 (**4 or less**).
- 2. The **10s digit value** will increase by **ten** (round up), if the digit in the **1s** column is a 5, 6, 7, 8, 9 (**5 or more**).
- 3. The **value** of any digits in the **column place values** to the **right** of the **10s** column change to a **place holder**, **0**.
- 4. The **value** of any digits in the **column place values** to the **left** of the **10s** column usually remain the **same**. (If the **10s** digit value increases to 100 then the **10s** digit becomes a **place holder**, **0** and the **100s** digit increases by 100 more)

### Step 1

First, write the number 3,257 on a Place Value Grid in the correct column place values of the 1s, 10s, 100s and 1,000s.

#### Step 2

Then, say the digit in the **1s** column which is **7** and as it is **5 or more** the **10s** digit value will increase by **ten** (round up).

Next, the digit value of the **5 tens** (50), add **10** to make **6 tens** (60). In the **10s** column write the digit **6** underneath the digit **5**.

### Step 4

Then, the 1s column digit value changes to a place holder, 0. In the 1s column write the digit 0 underneath the digit 7.

## Step 5

Next, the **1,000s** and **100s** column digit values remain the **same** as **3** and **2**. In the **1,000s** and **100s** columns write the same digits **3** and **2** underneath.

### Step 6

Finally, 3,257 rounded to the nearest 10 is 3,260.

### To Nearest 100

#### Place Value Grid

<u>1000s</u>	<u>100s</u>	<u>10s</u>	<u>1s</u>	•	<u>10ths</u>	<u>100ths</u>
5	4	7	9	•		
5	5	0	0	•		

#### **Strategy Applied**

When rounding to the nearest 100s place value, the following will occur.

- 1. The **100s digit value** will remain the **same** (round down), if the digit in the **10s** column is a 0, 1, 2, 3, 4 (**4 or less**).
- 2. The **100s digit value** will increase by **one hundred** (round up), if the digit in the **10s** column is a 5, 6, 7, 8, 9 (**5 or more**).
- 3. The value of any digits in the column place values to the right of the 100s column change to a place holder, 0.
- 4. The **value** of any digits in the **column place values** to the **left** of the **100s** column usually remain the **same**. (If the **100s** digit value increases to 1,000 then the **100s** digit becomes a **place holder**, **0** and the **1,000s** digit increases by 1,000 more)

#### Step 1

First, write the number **5,479** on a **Place Value Grid** in the correct column place values of the **1s**, **10s**, **100s** and **1,000s**.

#### Step 2

Then, say the digit in the **10s** column which is **7** and as it is **5 or more** the **100s** digit value will increase by **one hundred** (round up).

Next, the digit value of the **4 hundreds** (400), add **100** to make **5 hundreds** (500).

In the 100s column write the digit 5 underneath the digit 4.

## Step 4

Then, the **10s** and **1s** column digit values change to a **place holder**, **0**. In the **10s** and **1s** columns write the digit **0** underneath the digit **7** and **9**.

## Step 5

Next, the **1,000s** column digit value remains the **same** as **5**. In the **1,000s** column write the same digit **3** underneath.

### Step 6

Finally, 5,479 rounded to the nearest 100 is 5,500.

### To Nearest 1,000

#### Place Value Grid

<u>1000s</u>	<u>100s</u>	<u>10s</u>	<u>1s</u>	•	<u>10ths</u>	<u>100ths</u>
4	3	6	8	•	7	9
4	0	0	0	•	0	0

#### **Strategy Applied**

When rounding to the nearest 1,000s place value, the following will occur.

- 1. The **1,000s digit value** will remain the **same** (round down), if the digit in the **100s** column is a 0, 1, 2, 3, 4 (**4 or less**).
- 2. The **1,000s digit value** will increase by **one thousand** (round up), if the digit in the **100s** column is a 5, 6, 7, 8, 9 (**5 or more**).
- 3. The **value** of any digits in the **column place values** to the **right** of the **1,000s** column change to a **place holder**, **0**.
- 4. The value of any digits in the column place values to the left of the **1,000s** column usually remain the same. (If the **1,000s** digit value increases to 10,000 then the **1,000s** digit becomes a place holder, **0** and the **10,000s** digit increases by 10,000 more)

#### Step 1

First, write the number 4368.79 on a Place Value Grid in the correct column place values of the 100ths, 10ths, 1s, 10s, 100s and 1,000s.

### Step 2

Then, say the digit in the **100s** column which is **4** and as it is **4 or less** the **1,000s** digit value will remain the **same** (round down).

Next, the digit value of the 4 thousands (4,000) remains the same. In the 1,000s column write the digit 4 underneath the digit 4.

### Step 4

Then, the 100s, 10s, 1s, 10ths and 100ths column digit values change to a place holder, 0.

In the 100s, 10s, 1s, 10ths and 100ths columns write the digit 0 underneath the digits 3, 6, 8, 7 and 9.

### Step 5

Next, the **1,000s** column digit value remains the **same** as **4**. In the **1,000s** column write the same digits **4** underneath.

### Step 6

Finally, 4368.79 rounded to the nearest 1,000 is 4,000.

# Fraction of a Quantity

1) 
$$\frac{7}{8}$$
 of  $16 = ?$ 

#### Word Problem

A **sixteen** slice extra large pizza was shared between the **eight** Scouts. Only **seven** Scouts ate, eating some slices.

How many slices have been eaten?

### **Concrete Object**

Quantity

			_				
1	2	3	4	5	6	7	8
9	10	11	12	13	14	15	16

Group 1  1 2	Group 2	Group 3	Group 4
Group 5	Group 6	Group 7	Group 8

## **Strategy Applied**

A fraction is part of a **whole** or part of **1** and an **eighth** is 1 of 8 **equal groups**.

16 is the quantity shared equally between the total number of equal groups.

8 is the denominator, represents the total number of equal groups.

7 is the numerator, represents seven of the equal groups.

First, pick up **sixteen** objects and place them together. Now count aloud from 1 to 16, to check there are only **sixteen** objects.

Then, **share** the **sixteen** objects one at a time **equally between** the **eight** groups, until exactly the **same quantity** of objects are in **each** of the groups.

Next, count how many objects there are altogether in seven groups, there should be fourteen objects; one, two, three, four, five, six, seven, eight, nine, ten, eleven, twelve, thirteen, fourteen.

Finally, the missing number is **fourteen** objects, which is the **total** amount in **seven** of the groups.

#### **Bar Model**

			1	6			
2	2	2	2	2	2	2	2

1) 
$$\frac{7}{8}$$
 of 16 = \_\_\_\_

6) 
$$\frac{2}{5}$$
 of 25 = \_\_\_\_

2) 
$$\frac{2}{3}$$
 of 15 = \_\_\_\_

7) 
$$\frac{1}{3}$$
 of 27 = \_\_\_\_

3) 
$$\frac{3}{8}$$
 of 40 = \_\_\_\_

8) 
$$\frac{2}{5}$$
 of 30 = \_\_\_\_

4) 
$$\frac{2}{3}$$
 of 30 = \_\_\_\_

9) 
$$\frac{1}{3}$$
 of 24 = \_\_\_\_

5) 
$$\frac{4}{5}$$
 of 10 = \_\_\_\_

10) 
$$\frac{1}{2}$$
 of 52 = \_\_\_\_

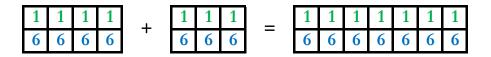
### **Add Fractions**

1) 
$$\frac{4}{6} + \frac{3}{6} = \frac{?}{?}$$

#### **Word Problem**

Popsy ate **four sixths** of a tin of cat food, whilst Jiggy ate **three sixths**. How many tins of cat food have they eaten?

### **Fraction Tiles**



## Step 1

## Step 2

$$\frac{4}{6} + \frac{3}{6} = \frac{4}{6} + \frac{3}{6} = \frac{7}{6}$$

## Step 3

$$= \frac{6}{6}$$
 or 1  $+ \frac{1}{6}$ 

## **Strategy Applied**

### Step 1

Add two fractions with the same denominators, **four-sixths** and **three-sixths**.

The 4 represents the **numerator**.

The 6 represents the denominator.

#### Step 2

Add the **numerators 4 + 3** equalling **7**.

The **denominator** remains the **same** as **6**.

The resulting fraction is seven-sixths. (an improper fraction)

### Step 3

Convert the improper fraction of seven-sixths into a mixed fraction.

A mixed fraction consists of a whole number and a proper fraction.

Out of seven-sixths a fraction wall shows six-sixths is equivalent to one whole and with a remainder of one-sixth . 1 1

1) 
$$\frac{4}{6} + \frac{3}{6} =$$

$$6) \frac{7}{8} + \frac{3}{8} = \underline{\hspace{1cm}}$$

$$\frac{4}{5} + \frac{2}{5} = \underline{\hspace{1cm}}$$

7) 
$$\frac{8}{9} + \frac{8}{9} =$$

3) 
$$\frac{4}{9} + \frac{7}{9} =$$

4) 
$$\frac{4}{7} + \frac{5}{7} =$$

9) 
$$\frac{4}{5} + \frac{3}{5} = \frac{1}{5}$$

5) 
$$\frac{6}{4} + \frac{2}{4} =$$

$$10)$$
 $\frac{2}{3} + \frac{2}{3} =$ \_\_\_\_

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## **Subtract Fractions**

1) 
$$\frac{9}{9} - \frac{6}{9} = \frac{?}{?}$$

#### Word Problem

Mum and dad enter a pie eating competition at the summer fete. Mum ate nine-ninths of a pie and dad ate six-ninths less. How much pie was eaten by dad?

#### **Fraction Tiles**

1	1	1	1	1	1	1	1	1		1	1	1	1	1	1	_	1	1	1
9	9	9	9	9	9	9	9	9	-	9	9	9	9	9	9	_	9	9	9

### Step 1

## Step 2

$$\frac{9 - 6}{9} = \frac{3}{9}$$

### Step 3

Common Factors of 
$$3 = 1, 3$$
  
 $9 = 1, 3, 9$ 

## **Strategy Applied**

## Step 1

Subtract two fractions with the **same denominators** and **different numerators** of **nine-ninths** and **six-ninths**.

The 9 represents the numerator.
The 9 represents the denominator.

The 6 represents the **numerator**.

The 9 represents the **denominator**.

Subtract the **numerators 9** - **6** equalling **3**.

The denominator remains the same as 9.

The resulting fraction is three-ninths. (Simplify if possible)

### Step 3

**Simplify** a fraction by reducing the **numerator** and **denominator** to their **lowest terms** by **dividing** them **both** by their **Highest Common Factor**.

The Highest Common Factor (HCF) of 3 and 9 is 3.

The value of the simplified fraction of  $\frac{1}{3}$ 

1) 
$$\frac{9}{9} - \frac{6}{9} =$$

6) 
$$\frac{2}{3} - \frac{1}{3} =$$

2) 
$$\frac{3}{8} - \frac{1}{8} =$$

7) 
$$\frac{1}{2} - \frac{1}{2} = \underline{\hspace{1cm}}$$

$$\frac{5}{6} - \frac{3}{6} = \underline{\phantom{0}}$$

$$8) \frac{8}{8} - \frac{4}{8} = \underline{\hspace{1cm}}$$

4) 
$$\frac{5}{6}$$
 -  $\frac{1}{6}$  = \_\_\_\_

9) 
$$\frac{3}{3} - \frac{1}{3} =$$

$$10)_{\frac{7}{9}} - \frac{1}{9} = \underline{\hspace{1cm}}$$

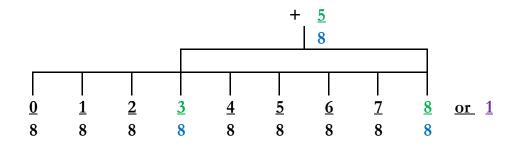
# Find the Missing Number

1) 
$$\frac{3}{8} + \frac{?}{?} = 1$$

### Word Problem

A litre bottle is **three eighths** full of water. How much water is required to fill the **bottle?** 

#### Number Line



## Fraction Tiles

1	1	1		1	1	1	1	1	_	1	1	1	1	1	1	1	1
8	8	8	'	8	8	8	8	8		8	8	8	8	8	8	8	8

## **Strategy Applied**

### Step 1

The 3 represents the numerator.

The 8 represents the **denominator**.

The 1 whole is equivalent to

8

First, draw a number line that represents **eighths**, writing **zero-eighths** at the start and **eight-eighths** or **one** whole at the end.

Then, number the number line by counting on one-eighth at a time.

Next, find and touch the number three-eighths on a number line.

Then, count forwards **one-eighth** at a time on a number line from the **three-eighths** on to **eight-eighths** or **one whole**.

Finally the number of **eighths** counted on is **five-eighths**, the missing number.

1) 
$$\frac{3}{8}$$
 +  $\frac{1}{8}$  = 1

$$2) \frac{5}{9} + \underline{\hspace{1cm}} = 1$$

3) 
$$1 \div \underline{\phantom{0}} = \underline{1}$$

5) 
$$2 \frac{1}{2} m + 4 m = ____$$

6) 
$$\frac{5}{12} + \frac{11}{12} = \frac{1}{12}$$

7) 
$$\frac{12}{5} - \frac{4}{5} = \underline{\hspace{1cm}} + 1$$

$$8) \quad \frac{2}{9} + \frac{8}{9} - \frac{4}{9} = \underline{\hspace{1cm}}$$

## P. 2

- 1) 1 thousand, 2 hundreds, 3 tens, 4 ones, 5 tenths, 6 hundredths
- 2) 1 thousand, 2 hundreds, 4 tens, 6 ones, 1 tenths, 9 hundredths
- 3) 2 thousand, 1 hundreds, 7 tens, 0 ones, 8 tenths, 3 hundredths
- 4) 3 thousand, 5 hundreds, 3 tens, 7 ones, 7 tenths, 4 hundredths
- 5) 4 thousand, 0 hundreds, 6 tens, 8 ones, 6 tenths, 1 hundredths
- 6) 5 thousand, 3 hundreds, 7 tens, 9 ones, 0 tenths, 2 hundredths
- 7) 6 thousand, 5 hundreds, 1 tens, 3 ones, 9 tenths, 3 hundredths
- 8) 7 thousand, 2 hundreds, 1 tens, 5 ones, 4 tenths, 8 hundredths
- 9) 8 thousand, 3 hundreds, 4 tens, 6 ones, 5 tenths, 7 hundredths
- 10) 9 thousand, 5 hundreds, 3 tens, 7 ones, 2 tenths, 0 hundredths

<u>P. 4</u>	<u>P. 6</u>	<u>P. 8</u>
1) 1,000, 200, 30, 4, 0.5, 0.06	1) 2,750	1) 1,980
2) 1,000, 200, 40, 6, 0.1, 0.09	2) 3,559	2) 2,470
3) 2,000, 100, 70, 9, 0.8, 0.03	3) 4,699	3) 2,150
4) 3,000, 500, 30, 7, 0.7, 0.04	4) 5,455	4) 2,090
5) 4,000, 0, 60, 8, 0.6, 0.01	5) 6,308	5) 2,550
6) 5,000, 300, 70, 9, 0.0, 0.02	<b>6)</b> 7 <b>,</b> 700	6) 2,180
7) 6,000, 500, 10, 3, 0.9, 0.03	7) 8,619	7) 3,330
8) 7,000, 200, 10, 5, 0.4, 0.08	8) 9,591	8) 4,330
9) 8,000, 300, 40, 6, 0.5, 0.07	9) 10,455	9) 5,380
10) 9,000, 500, 30, 7, 0.8, 0.00	10) 10,309	10) 6,210
	11) 1,309	11) 5,720
	12) 1,455	12) 4,050
	13) 1,591	13) 3,990
	14) 1,710	14) 9,740

<u>P. 10</u>	<u>P. 12</u>	<u>P. 14</u>	<u>P. 16</u>
1) 850	1) 900	1) 18, 24	1) 3.9
2) 760	2) 2,400	2) 42, 48	2) 3.8
3) 640	3) 1,200	3) 58, 64	3) 8.9
4) 520	4) 3,600	4) 21, 28	4) 8.9
5) 810p	5) 7,000	5) 49, 56	5) 7.9
6) 730p	6) 10,000	6) 71, 78	6) 6.8
7) £700	7) 8,000	7) 27, 36	7) 8.1
8) £500	8) £1,800	8) 63, 72	8) 10.0
9) 900	9) 900cm	9) 37, 46	9) 10.0
10) 380	10) 1,500m	10) 75, 100	10) 6.8
11) 750	11) 2,200	11) 95, 120	11) 7.6
12) 430	12) 4,500	12) 175, 200	12) 10.00
13) 520	13) 2,500	13) 315, 415	13) 7.2
14) 350	14) 9,000	14) 683, 783	14) 9.1
<u>P. 18</u>	<u>P. 20</u>	<u>P. 22</u>	<u>P. 24</u>
1) 6,081	1) 74.24	1) 1,300	1) 280
2) 5,385	2) 62.85	2) 2,642	2) 1,520
3) 7,520	3) 91.04	3) £4.20	3) 2,489
4) 9,722	4) 86.22	4) £11.39	4) 3,345
5) 9,762	5) 74.62	5) 1hr 37min	5) 4,250
6) 9,374	6) 95.72	6) 1m 350cm	6) 5,222
7) 7,909	7) 153.09	7) 1,743ml	7) 6,340
8) 3,748	8) 91.08	8) 5,371	8) 7,400
9) 17,634	9) 186.24	9) 0.64	9) 8,690
10) 7,872	10) 108.72	10) 30	10) 8,710
11) 7,693	11) 86.93	11) 42	11) 210
12) 6,386	12) 183.86	12) 81	12) 3,784
13) 7,465	13) 22.65	13) 300	13) 6,969
14) 18,846	14) 198.36	14) 425	14) 8,907

<u>P. 26</u>	<u>P. 28</u>	<u>P. 30</u>	<u>P. 32</u>
1) 4,950	1) 625	1) 4,000	1) 6, 0
2) 3,800	2) 865	2) 1,000	2) 21, 15
3) 5,120	3) 547	3) 700	3) 33, 27
4) 1,340	4) 500	4) 700	4) 31, 24
5) 2,420	5) 480	5) 1,900	5) 43, 36
6) 3,420	6) 865	6) 1,800	6) 55, 48
7) 6,130	7) 542	7) 3,800	7) 74, 65
8) 5,600	8) 400	8) 4,500	8) 183, 174
9) 9,420	9) 280	9) 1,600	9) 278, 269
10) 4,960	10) 543	10) 2,000	10) 393, 384
11) 1,550	11) 765	11) 740	11) 650, 625
12) 5,860	12) 816	12) 2,850	12) 875, 850
13) 1,540	13) 494	13) 2,930	13) 900, 800
14) 3,300	14) 632	14) 5,700	14) 2,400, 2,30
D 04	D 40	D 40	D 40
<u>P. 34</u>	<u>P. 38</u>	<u>P. 40</u>	<u>P. 42</u>
1) 0.3	1) 6,792	1) 54.9	1) 9,700
2) 1.2	2) 3,492	2) 20.9	2) 2,832
3) 3.7	3) 2,874	3) 44.9	3) 3,000
4) 6.1			
•	4) 1,189	4) 49.2	4) £1.70
5) 4.5	5) 3,589	5) 19.6	5) 776
•	· ·	,	
5) 4.5	5) 3,589	5) 19.6	5) 776
5) 4.5 6) 2.6	5) 3,589 6) 3,469	5) 19.6 6) 17.4	5) 776 6) 719
5) 4.5 6) 2.6 7) 0.7	5) 3,589 6) 3,469 7) 6,771	5) 19.6 6) 17.4 7) 27.1	5) 776 6) 719 7) 6,523
5) 4.5 6) 2.6 7) 0.7 8) 2.2	5) 3,589 6) 3,469 7) 6,771 8) 2,802	5) 19.6 6) 17.4 7) 27.1 8) 28.2	5) 776 6) 719 7) 6,523 8) £27.21
5) 4.5 6) 2.6 7) 0.7 8) 2.2 9) 6.2	5) 3,589 6) 3,469 7) 6,771 8) 2,802 9) 7.797	5) 19.6 6) 17.4 7) 27.1 8) 28.2 9) 9.7	5) 776 6) 719 7) 6,523 8) £27.21 9) 57
5) 4.5 6) 2.6 7) 0.7 8) 2.2 9) 6.2 10) 0.4	5) 3,589 6) 3,469 7) 6,771 8) 2,802 9) 7.797 10) 552	5) 19.6 6) 17.4 7) 27.1 8) 28.2 9) 9.7 10) 23.6	5) 776 6) 719 7) 6,523 8) £27.21 9) 57 10) 24
5) 4.5 6) 2.6 7) 0.7 8) 2.2 9) 6.2 10) 0.4 11) 3.2	5) 3,589 6) 3,469 7) 6,771 8) 2,802 9) 7.797 10) 552 11) 1,062	5) 19.6 6) 17.4 7) 27.1 8) 28.2 9) 9.7 10) 23.6 11) 11.9	5) 776 6) 719 7) 6,523 8) £27.21 9) 57 10) 24 11) 45
5) 4.5 6) 2.6 7) 0.7 8) 2.2 9) 6.2 10) 0.4 11) 3.2 12) 3.4	5) 3,589 6) 3,469 7) 6,771 8) 2,802 9) 7.797 10) 552 11) 1,062	5) 19.6 6) 17.4 7) 27.1 8) 28.2 9) 9.7 10) 23.6 11) 11.9 12) 27.0	5) 776 6) 719 7) 6,523 8) £27.21 9) 57 10) 24 11) 45 12) 56
5) 4.5 6) 2.6 7) 0.7 8) 2.2 9) 6.2 10) 0.4 11) 3.2 12) 3.4 13) 3.8	5) 3,589 6) 3,469 7) 6,771 8) 2,802 9) 7.797 10) 552 11) 1,062	5) 19.6 6) 17.4 7) 27.1 8) 28.2 9) 9.7 10) 23.6 11) 11.9 12) 27.0 13) 20.6	5) 776 6) 719 7) 6,523 8) £27.21 9) 57 10) 24 11) 45 12) 56 13) 72

<u>P. 44</u>	<u>P. 46</u>	<u>P. 48</u>	<u>P. 50</u>
1) 48	1) 40	1) 2,600	1) 112
2) 36	2) 75	2) 390	2) 272
3) 36	3) 30	3) 4,100	3) 1,070
4) 25	4) 120	4) 580	4) 8,540
5) 77	5) 48	5) 6,300	5) 423
6) 16	6) 147	6) 720	6) 312
7) 96	7) 42	7) 8,000	7) 1,125
8) 36	8) 96	8) 940	8) 41,285
9) 27	9) 72	9) 7,500	9) 387
10) 48	10) 84	10) 530	10) 189
11) 81	11) 420	11) 9,100	11) 704
12) 44	12) 960	12) 820	12) 66,060
13) 24	13) 7,200	13) 6,400	
14) 42	14) 84,000	14) 550	
<u>P. 52</u>	<u>P. 54</u>	<u>P. 56</u>	<u>P. 58</u>
1) 64.05	1) 200	1) 3	1) 3.61
2) 330.96	2) 6	2) 9	2) 32.9
3) 372.33	<b>3</b> ) 0	3) 9	3) 3.38
4) 412.85	4) 240	4) 46	4) 48.2
5) 128.37	5) 72	5) 4	5) 1.23
6) 367.00	6) 147	6) 98	6) 72.4
7) 660.60	7) 12	7) 30	7) 1,35
8) 260.80	8) 72	8) 96	8) 16.6
9) 372.36	9) 6	9) 110	9) 2.47
10) 424.32	10) 256	10) 56	10) 920.8
11) 434.42	11) 15	11) 2	11) 41.59
12) 402.16	<b>12)</b> 0	12) 7	12) 610.7
	13) 12	13) 12	13) 52.03
	14) 690	14) 11	14) 310.9
8) 36 9) 27 10) 48 11) 81 12) 44 13) 24 14) 42 P. 52 1) 64.05 2) 330.96 3) 372.33 4) 412.85 5) 128.37 6) 367.00 7) 660.60 8) 260.80 9) 372.36 10) 424.32 11) 434.42	8) 96 9) 72 10) 84 11) 420 12) 960 13) 7,200 14) 84,000  P. 54 1) 200 2) 6 3) 0 4) 240 5) 72 6) 147 7) 12 8) 72 9) 6 10) 256 11) 15 12) 0 13) 12	8) 940 9) 7,500 10) 530 11) 9,100 12) 820 13) 6,400 14) 550  P. 56 1) 3 2) 9 3) 9 4) 46 5) 4 6) 98 7) 30 8) 96 9) 110 10) 56 11) 2 12) 7 13) 12	8) 41,285 9) 387 10) 189 11) 704 12) 66,060  P. 58 1) 3.61 2) 32.9 3) 3.38 4) 48.2 5) 1.23 6) 72.4 7) 1,35 8) 16.6 9) 2.47 10) 920.8 11) 41.59 12) 610.7 13) 52.03

<u>P. 60</u>	<u>P. 62</u>	<u>P. 64</u>	<u>P. 66</u>
1) 228 r1	1) 5.69	1) 4	1) 5
2) 2,712 r1	2) 4.12 r1	2) 2	2) 1
3) 3,567 r1	3) 8.85 r2	3) 0.07	3) 3
4) 125 r1	4) 7.19 r3	4) 0.26	4) 12
5) 1,069 r3	5) 8.85	5) 4	5) -8
6) 2,752 r1	6) 4.12	6) 11	6) -14
7) 14 r5	7) 6.00 r4	7) 0.3	7) -7
8) 1,852	8) 4.17 r4	8) 0.6	8) -12
9) 1,835	9) 5.93 r5	9) 7	9) -13
10) 91 r3	10) 2.12 r1	10) 8	10) -15
11) 701		11) 26	11) -7
12) 460 r4		12) 14	12) 8
13) 33 r4		13) 8	13) 9
14) 646 r5		14) 9	14) 11
15) 656 r2			
<u>P. 68</u>	<u>P. 70</u>	<u>P. 72</u>	<u>P. 74</u>
1) 3,260	1) 5,500	1) 4,000	1) 14
2) 2,140	2) 900	2) 1,000	2) 10
3) 7,660	3) 9,900	3) 9,000	3) 15
4) 7,220	4) 5,900	4) 6,000	4) 20
5) 4,400	5) 2,200	5) 3,000	5) 8
6) 3,200	6) 1,100	6) 2,000	6) 10
7) 40.00	7) 100.00	7) 8,000	7) 9
8) 10.00	8) 200.00	8) 7,000	8) 12
9) 90.00	9) 400.00	9) 4,000	9) 8
10) 60.00	10) 600.00	10) 10,000	10) 26
11) 30.00	11) 600.00	11) 2,000	
12) 20.00	12) 700.00	12) 6,000	
13) 870.00	13) 9,900.00	13) 1,000	
14) 1,250.00	14) 9,400.00	14) 10,000	

**P.** 76

1) 
$$\frac{7}{8}$$
 or  $\frac{1}{6}$ 

1) 
$$\frac{7}{8}$$
 or  $\frac{1}{6}$   $\frac{1}{8}$  or  $\frac{1}{2}$   $\frac{2}{8}$ 

2) 
$$\frac{6}{5}$$
 or  $1\frac{1}{5}$ 

2) 
$$\frac{6}{5}$$
 or  $\frac{1}{5}$   $\frac{1}{5}$  7)  $\frac{16}{9}$  or  $\frac{1}{7}$ 

3) 
$$\frac{11}{9}$$
 or  $\frac{2}{9}$ 

3) 
$$\frac{11}{9}$$
 or  $\frac{1}{2}$  8)  $\frac{12}{7}$  or  $\frac{1}{5}$ 

4) 
$$\frac{9}{7}$$
 or  $\frac{1}{7}$ 

5) 
$$\frac{8}{4}$$
 or 2

10) 
$$\frac{4}{3}$$
 or  $\frac{1}{3}$ 

$$9 \frac{3}{9} \text{ or } \frac{1}{3}$$
 6)  $\frac{1}{3}$ 

3) 
$$\frac{2}{6}$$
 or  $\frac{1}{3}$  8)  $\frac{4}{8}$  or  $\frac{1}{2}$ 

8) 
$$\frac{4}{8}$$
 or  $\frac{1}{2}$ 

8) 
$$\frac{6}{9}$$
 or  $\frac{1}{3}$ 

5) 
$$\frac{2}{4}$$
 or  $\frac{1}{2}$  10)  $\frac{6}{9}$  or  $\frac{2}{3}$ 

**Common Factor** is a number which is a factor of two or more other numbers, e.g. 3 is a common factor of the numbers 9 and 30.

**Common Multiple** is an integer which is a multiple of a given set of integers, e.g. 24 is a common multiple of 2, 3, 4, 6, 8 and 12.

**Decimal Fraction** is tenths, hundredths, thousandths etc. represented by digits following a decimal point. E.g. 0.125 is equivalent to 1/10 + 2/100 + 5/1000 or 1/8. The decimal fraction representing 1/8 is a terminating decimal fraction since it has a finite number of decimal places. Other fractions such as 1/3 produce recurring decimal fractions, these have a digit or group of digits that is repeated indefinitely.

**Denominator** is the number written below the line i.e. the divisor. e.g. in the fraction  $\frac{2}{3}$  the denominator is 3.

**Digit Value** is the value of a digit that relates to its position or place in a number. e.g. in 82 the digits represent 8 tens and 2 ones.

**Equivalent Fraction** are fractions with the same value as another. e.g. 4/8, 5/10, 8/16 are all equivalent fractions and all are equal to 1/2.

**Exchanging** is to exchange a number for another of equal value. The process of regrouping is used in some standard compact methods of calculation. e.g.: 'carrying figures/exchanging' in addition, multiplication or division; and 'decomposition' in subtraction.

**Factor** is when a number, can be expressed as the product of two numbers, these are factors of the first. E.g. 1, 2, 3, 4, 6 and 12 are all factors of 12 because  $12 = 1 \times 12 = 2 \times 6 = 3 \times 4$ .

**Highest Common Factor (H.C.F.)** is the common factor of two or more numbers which has the highest value.

e.g. 16 has factors 1, 2, 4, 8, 16. 24 has factors 1, 2, 3, 4, 6, 8, 12, 24. 56 has factors 1, 2, 4, 7, 8, 14, 28, 56. The common factors of 16, 24 and 56 are 1, 2, 4 and 8. Their highest common factor is 8.

**Improper Fraction** is an improper fraction has a numerator that is greater than its denominator. Example: 9/4 is improper and could be expressed as the mixed number 2 1/4.

**Integer** is any of the positive or negative whole numbers and zero. e.g. ...2, -1, 0, +1, +2 ...

**Lowest Common Multiple (L.C.M.)** is the common multiple of two or more numbers, which has the least value. E.g. 3 has multiples 3, 6, 9, 12.... 4 has multiples 4, 8, 12, 16, 20, 24 ... and 6 has multiples 6, 12, 18, 24, 30 .... The common multiples of 3, 4 and 6 include 12, 24 and 36.

The lowest common multiple of 3, 4 and 6 is 12.

**Mixed Fraction** is a whole number and a fractional part expressed as a common fraction. e.g. 1 1/3 is a mixed fraction or mixed number.

**Mixed Number** is a whole number and a fractional part expressed as a common fraction. Example: 2 ½ is a mixed number. Also known as a mixed fraction.

**Multiple** is the result of multiplying a number by an integer, e.g. 12 is a multiple of 3 because  $3 \times 4 = 12$ .

**Non-Unit Fraction** is a fraction that has a value of 2 or more as the numerator and whose denominator is a non-zero integer. e.g. 1/2, 1/3.

**Numerator** is the number written on the top— the dividend (the part that is divided). In the fraction 2/3, the numerator is 2.

**Operations** that, when they are combined, leave the entity on which they operate unchanged. Examples: addition and subtraction are inverse operations e.g. 5 + 6 - 6 = 5. Multiplication and division are inverse operations e.g.  $6 \times 10 \div 10 = 6$ .

**Partition** 1) To separate a set into subsets. 2) To split a number into component parts. e.g. the two-digit number 38 can be partitioned into 30 + 8 or 19 + 19. 3) A model of division. e.g.  $21 \div 7$  is treated as 'how many sevens in 21?'

**Percentage** 1) A fraction expressed as the number of parts per hundred and recorded using the notation %. E.g. One half can be expressed as 50%; the whole can be expressed as 100% 2) Percentage can also be interpreted as the operator 'a number of hundredths of'.

**Place Holder** In decimal notation, the zero numeral is used as a place holder to denote the absence of a power of 10.

**Place Value** is the value of a digit that relates to its position or place in a number. e.g. in 1482 the digits represent 1 thousand, 4 hundred, 8 tens and 2 ones respectively; in 12.34 the digits represent 1 ten, 2 ones, 3 tenths and 4 hundredths respectively.

**Proper Fraction** has a numerator that is less than its denominator, so 3/4 is a proper fraction, whereas 4/3 is an improper fraction (i.e. not proper).

**Regrouping** is to exchange a number for another of equal value. The process of regrouping is used in some standard compact methods of calculation. e.g.: 'carrying figures/exchanging' in addition, multiplication or division; and 'decomposition' in subtraction.

**Remainder** in the context of division requiring a whole number answer (quotient), the amount remaining after the operation. e.g. 29 divided by 7 = 4 remainder 1.

**Simplify Fraction** is to simplify a fraction down to its lowest terms. The numerator and denominator are divided by the same number e.g. 4/8 = 2/4, also to 'reduce' a fraction.

When the numerator and denominator are both divided by their highest common factor the fraction is said to have been cancelled down to give the equivalent fraction in its lowest terms. e.g. 18/30 = 3/5 (dividing numerator and denominator by 6).

**Unit Fraction** is a fraction that has 1 as the numerator and whose denominator is a non-zero integer. e.g.1/2, 1/3.