Year 1 Arithmetic Workbook

by Richard Brown

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Key Language and Representations

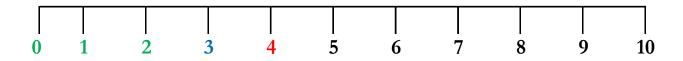
Word Problems are the arithmetic number sentences written in a real-life reasoning and problem solving scenario. e.g. 3 + 4 = 7

Strategy Applied refers to when a formal written method is used to calculate a number sentent 25 - 5 = 20

Explained using appropriate mathematical language, proven using concrete objects that can be handled, shown with pictorial representations visualising the calculations, to ensure a greater understanding of a mathematical concept.

Concrete Objects are manipulated or handled to calculate and represent a number sentence i.e. multilink cubes, numicon, counters, number line.

Number Lines are used to count forwards e.g. 0, 1, 2, 3, 4, 5 and also to count backwards e.g. 10, 9, 8, 7, 6, 5.



Part Whole Models are pictorial mathematical images to represent varied calculations and number sentences.

e.g.
$$6 + 3 = \frac{?9}{3}$$
 e.g. 9

Bar Models are an image, that pictorially represents a number sentence.

e.g. $3 + 9 = \frac{?}{12}$



2 = ?18

e.g. **20** -

9

Number Grid

0	1	2	3	4	5	6	7	8	9
10	11	12	13	14	15	16	17	18	19
20	21	22	23	24	25	26	27	28	29
30	31	32	33	34	35	36	37	38	39
40	41	42	43	44	45	46	47	48	49
50	51	52	53	54	55	56	57	58	59
60	61	62	63	64	65	66	67	68	69
70	71	72	73	74	75	76	77	78	79
80	81	82	83	84	85	86	87	88	89
90	91	92	93	94	95	96	97	98	99
100	101	102	103	104	105	106	107	108	109
110	111	112	113	114	115	116	117	118	119
120	121	122	123	124	125	126	127	128	129
130	131	132	133	134	135	136	137	138	139
140	141	142	143	144	145	146	147	148	149
150	151	152	153	154	155	156	157	158	159

Multiplication Square

X	2	3	4	5	6	7	8	9	10
0	0	0	0	0	0	0	0	0	0
1	2	3	4	5	6	7	8	9	10
2	4	6	8	10	12	14	16	18	20
3	6	9	12	15	18	21	24	27	30
4	8	12	16	20	24	28	32	36	40
5	10	15	20	25	30	35	40	45	50
6	12	18	24	30	36	42	48	54	60
7	14	21	28	35	42	49	56	63	70
8	16	24	32	40	48	56	64	72	80
9	18	27	36	45	54	63	72	81	90
10	20	30	40	50	60	70	80	90	100
11	22	33	44	55	66	77	88	99	110
12	24	36	48	60	72	84	96	108	120

How Many

How many 10s (tens) and 1s (ones) are there in the number 14?

Word Problem

The number **fourteen** is a **2-digit number**.

Each of the **digits** represents the **10s** and **1s column place values**.

Work out how many 10s and 1s, there are in the number fourteen?

Place Value Grid

<u>Hundreds</u>	<u>Tens</u>	<u>Ones</u>
<u>100s</u>	<u>10s</u>	<u>1s</u>
	1	4

Strategy Applied

The number **fourteen** is to be represented on a **Place Value Grid**. In **14**, the **4** represents the amount of **ones** in the **1s** column place value. In **13**, the **1** represents the amount of **tens** in the **10s** column place value.

First, write 4 in the 1s column place value, representing the amount of ones.

Then, write 1 in the 10s column place value, representing the amount of tens.

Finally, we can see from the columns of the **Place Value Grid** that the number **fourteen** represents **1 ten** and **4 ones**.

Test Questions

In each number, how many 10s (tens) and 1s (ones) are there?

- 1) 14 = ____
- 2) 15 = ____
- 3) 17 = ____
- 4) 19 = ____
- 5) 20 = ____
- 6) 23 = ____
- 7) 24 = ____
- 8) 32 = ____
- 9) 45 = ____
- 10) 57 = ____
- 11) 69 = ____
- 12) 70 = ____
- 13) 83 = ____
- 14) 94 = ____

Digit Value

What is the digit value of the 1s (ones) and 10s (tens) in the number 14?

Word Problem

The number **fourteen** is a **2-digit number**.

Each of the digits represents the 10s and 1s column place values.

What is the **digit value** of the 1 and 4 in the number **fourteen**?

Place Value Grid

<u>Hundreds</u>	<u>Tens</u>	<u>Ones</u>
<u>100s</u>	<u>10s</u>	<u>1s</u>
	10	4

Strategy Applied

The number fourteen is to be represented on a Place Value Grid.

In 14, the 4 represents the digit value of the ones in the 1s column place value.

In 14, the 1 represents the digit value of the tens in the 10s column place value.

First, write 4 in the 1s column place value, representing the value of the ones.

Then, write 10 in the 10s column place value, representing the value of the tens.

Finally, we can see from the columns of the **Place Value Grid** that the digit value of the 4 in the number **fourteen** remains the same as, 4 and the digit value of the 1 in the number **fourteen** is ten times as big as, 10.

Test Questions

What is the digit value of the 10s (tens) and 1s (ones) in each number?

- 1) 14 = ____
- 2) 15 =
- 3) 17 =
- 4) 19 = ____
- 5) 20 =
- 6) 23 =
- 7) 24 =
- 8) 32 = ____
- 9) 45 = ____
- 10) 57 = ____
- 11) 69 = ____
- 12) 70 =
- 13) 83 = ____
- 14) 94 = ____

1 More Than

Word Problem

Ameera puts together one cube and one cube.

Altogether how many cubes does she have?

Concrete Object



Strategy Applied

First, pick up one object and place it down.

Now count aloud to check there is only **one** object; **one**.

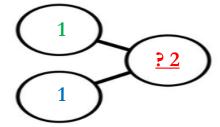
Then, pick up one more object and place it next to the one object.

Next, count how many objects there are altogether.

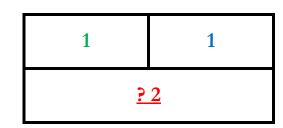
Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**.

Finally, one add one equals two.

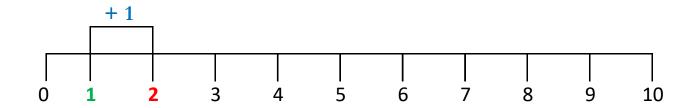
Part Whole Model



Bar Model



Number Line



Strategy Applied

First, find and touch the number one on the number line.

Then, **count forwards one** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be two.

Finally, one add one equals two.

6) One more than 5 is
$$=$$

$$2)$$
 4 + 1 =

9)
$$27cm + 1cm = ___$$

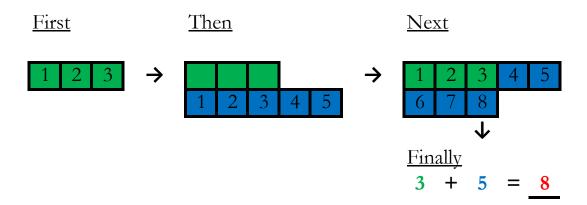
More Than 1

Word Problem

Tim has **three** cubes and Rachel has **five** cubes. they **put together** all of their cubes.

Altogether how many cubes do they have?

Concrete Object



Strategy Applied

First, pick up three objects and place them together.

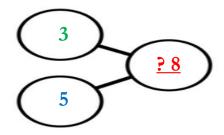
Now count aloud to check there are only three objects; one, two, three.

Then, pick up five more objects and place them next to the three objects.

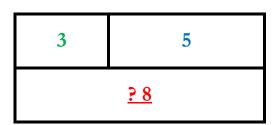
Next, count how many objects there are altogether.

Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**, **seven**, **eight**.

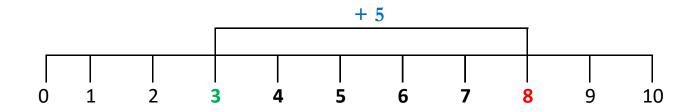
Finally, three add five equals eight.



Bar Model



Number Line



Strategy Applied

First, find and touch the number three on the number line.

Then, **count forwards five** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be eight.

Finally, three add five equals eight.

7)
$$9 \text{ cm} + 10 \text{cm} =$$

8)
$$16m + 3m =$$

$$4) 9 + 6 =$$

5)
$$7m_1 + 7m_2 =$$

More Than 1

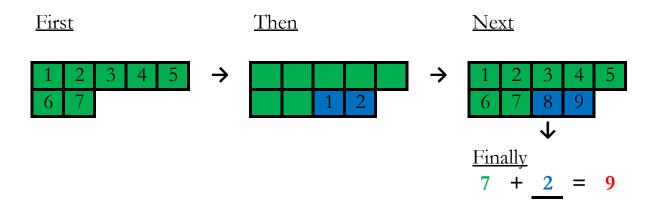
Word Problem

Kamal has **seven** objects and he is **given** some **more**.

Altogether he now has nine objects.

How many objects were given to him?

Concrete Object



Strategy Applied

First, pick up seven objects and place them together.

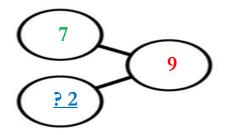
Now count aloud to check there are only seven objects; one, two, three, four, five, six, seven.

Then, count aloud from the next number after seven on to nine, 8, 9. As two numbers were counted on, pick up two more objects and place them next to the seven objects.

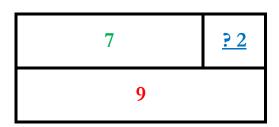
Next, count how many objects there are altogether.

Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**, **seven**, **eight**, **nine**.

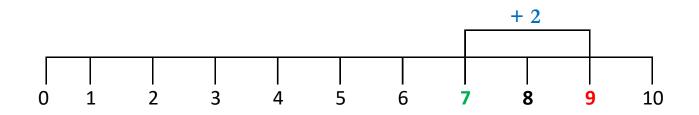
Finally, seven add two equals nine.



Bar Model



Number Line



Strategy Applied

First, find and touch the number seven on the number line.

Then, **count forwards two** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be nine.

Finally, seven add two equals nine.

$$1) \quad 7 \quad + \quad = \quad 9$$

$$2)$$
 4 + = 6

$$3) \quad 4 \quad + \quad = \quad 9$$

$$4) + 9 = 11$$

8)
$$13ml = 5ml +$$

9)
$$20ml = + 4ml$$

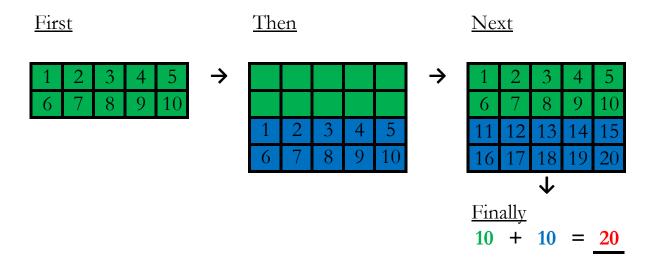
$$10)30L = _{--} + 14L$$

10 More

Word Problem

Mica has ten blocks and she picks up ten more blocks. How many blocks does she have altogether?

Concrete Object



Strategy Applied

First, pick up ten objects and place them together.

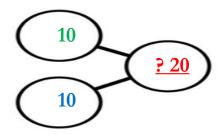
Now count aloud to check there are only ten objects; 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.

Then, pick up ten more objects and place it next to the ten objects.

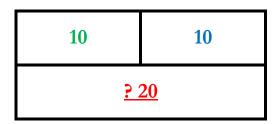
Next, count how many objects there are altogether.

Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**, **seven**, **eight**, nine, **ten**, **eleven**, **twelve**, **thirteen**, **fourteen**, **fifteen**, **sixteen**, **seventeen**, **eighteen**, **nineteen**, **twenty**.

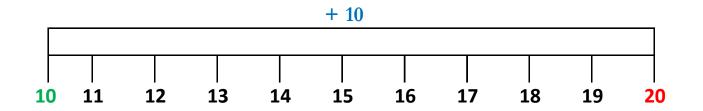
Finally, ten add ten equals twenty.



Bar Model



Number Line



Strategy Applied

First, find and touch the number ten on the number line.

Then, **count forwards ten** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be **twenty**.

Finally, ten add ten equals twenty.

$$3) 30 + 10 =$$

$$4) 60 + 10 =$$

$$6)$$
 $40 + 10 =$

8)
$$20g + 10g =$$

9)
$$90g + 10g =$$

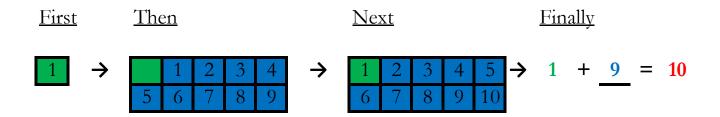
10)
$$100 \text{kg} + 10 \text{kg} =$$

Bonds to 10 and 20

Number bonds to 10, means two or more numbers added together that make the number **10**.

Number bonds to 20, means two or more numbers added together that make the number 20.

Concrete Object



Strategy Applied

First, pick up one object and place it down.

Now count aloud to check there is only **one** object; **one**.

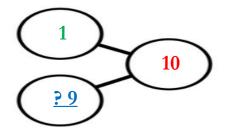
Then, count aloud from the next number after one on to ten, 2, 3, 4, 5, 6, 7, 8, 9, 10.

As **nine** numbers were counted on, pick up **nine** more objects and place them next to the **one** object.

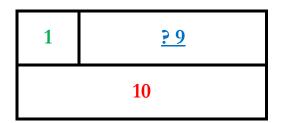
Next, count how many objects there are altogether.

Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**, **seven**, **eight**, **nine**, **ten**.

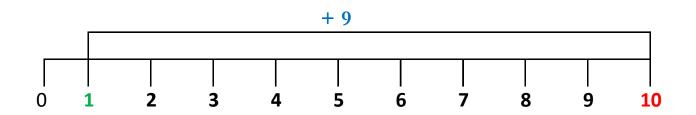
Finally, one add nine equals ten.



Bar Model



Number Line



Strategy Applied

First, find and touch the number one on the number line.

Then, **count forwards** aloud from the next number after **one** on to **ten** in number order, whilst touching the numbers on the number line.

Next, the amount of numbers counted on should be nine.

Finally, one add nine equals ten.

$$2) \quad 3 \quad + \quad = 10$$

$$3) \quad 5 \quad + \quad = \quad 10$$

$$4) \quad 7 \quad + \quad = 10$$

$$5)$$
 ___ + $8p$ = $10p$

$$6)$$
 ___ + $6p$ = $10p$

$$7)$$
 ___ + £14 = £20

$$8)$$
 ___ + £12 = £20

$$9) + 0 = 20$$

$$10)_{--} + 8 = 20$$

Page 14

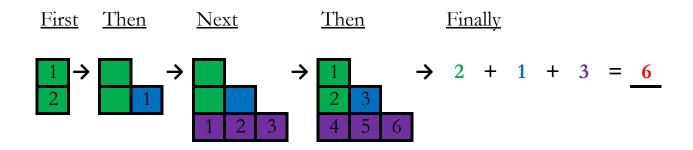
Multiple Numbers

Word Problem

Three friends have sweets. Sue has **two** sweets and Daniel has **one** sweet and Peter has **three** sweets.

How many sweets do they have altogether?

Concrete Object



Strategy Applied

First, pick up two objects and place them together.

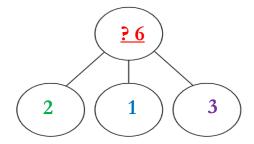
Then, pick up one more object and place it next to the two objects.

Next, pick up three more objects and place them next to the two and one objects.

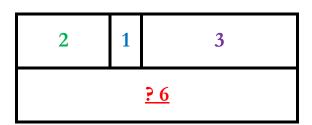
Then, count how many objects there are altogether.

Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**.

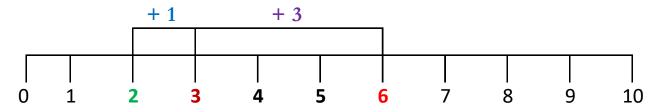
Finally, two add one add three equals six.



Bar Model



Number Line



Strategy Applied

First, find and touch the number two on the number line.

Then, **count forwards one** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be three.

Then, **count forwards three** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be six.

Finally, two add one add three equals six.

$$3)$$
 $5 + 5 + 7 = ____$

$$4)$$
 6 $+$ 6 $+$ 2 $=$

9)
$$50 \sec s + 10 \sec s + 10 \sec s =$$

$$5)$$
 $8 + 3 + 9 =$

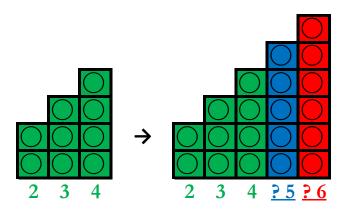
Multiples of 1, 2, 5 and 10

In the **number pattern** below, find the next two missing numbers.

Word Problem

Shannon uses cubes to make the **number pattern** of **two**, **three** and **four**. She calculates the next two missing numbers in the number pattern. How many cubes will she need, to make the next two numbers?

Concrete Object



Strategy Applied

Work out the **number pattern**, by finding out the **difference between** the **three** numbers.

The difference between each of the three numbers is known as the rule.

First, **count forwards** from **two** to **three** equalling **one**, the rule is **+1**.

Then, count forwards from three to four equalling one, the rule is +1.

The rule is **+1**, **count on one** from each of the numbers in the number pattern.

Continue this number pattern to find the next two missing numbers.

Next, find four on the number line and count on one more, total is five.

Then, find five on the number line and count on one more, total is six.

Finally, the next two missing numbers in the number pattern are **five** and **six**.

Number Line

Test Questions

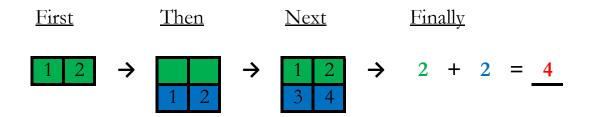
In each **sequence** of numbers, find the next two missing numbers.

Doubling

Word Problem

Child A and Child B, both have **two** objects **each**. How many objects do they have in **total?**

Concrete Object



Strategy Applied

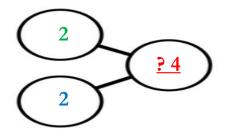
First, pick up **two** objects and place them together. Now count aloud to check there is only **two** objects; **one**, **two**.

Then, pick up two more object and place it next to the two objects.

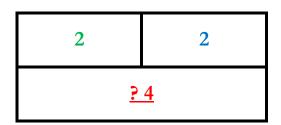
Next, count how many objects there are **altogether**. Whilst touching each object **count forwards** aloud in number order,

saying one number name per object; one, two, three, four.

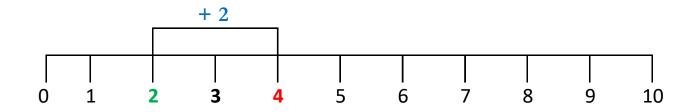
Finally, double two equals four.



Bar Model



Number Line



Strategy Applied

First, find and touch the number two on the number line.

Then, **count forwards two** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be **four**.

Finally, double two equals four.

$$1) \quad 2 \quad + \quad 2 \quad = \quad$$

$$3) \quad 6 \quad + \quad 6 \quad =$$

$$4) 1 + 1 =$$

$$6) \quad 5 \quad + \quad 5 \quad =$$

$$8) 10 + 10 =$$

$$9) \quad 0 \quad + \quad 0 \quad =$$

Find The Missing Number

1)
$$4 + 3 + ? = 9$$

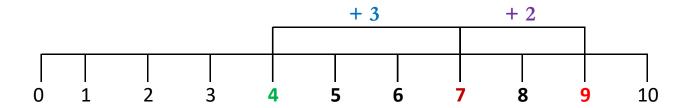
Word Problem

In a classroom, there are **four** boys and **three** girls sat down at their tables. There are **more** children sat on the carpet.

Altogether there are nine children in the classroom.

How many children are sat on the carpet?

Number Line



Strategy Applied

First, find and touch the number four on the number line.

Then, **count forwards three** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be **seven**.

Then, from **seven** count forwards aloud in number order, whilst touching the numbers on the number line, on to the number **nine**.

Next, say how many numbers were **counted on**, it should be **two** more.

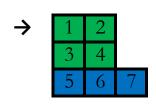
Finally, the **value** of the missing number is **two**.

Concrete Object

<u>First</u> <u>Then</u>

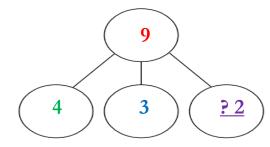
Next Finally



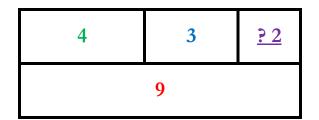


4	+	3	+	?	=	9

Part Whole Model



Bar Model



$$2)$$
 $7 + 2 + = 15$

$$3) + 4 + 12 = 22$$

4)
$$15 + \underline{\hspace{1cm}} + 10 = 29$$

$$5)$$
 ____ + 3 + 8 = 18

$$8) 16 = 9 + _ + 2$$

9)
$$20 = 1 + 10$$

$$10) \ 25 = + 12 + 7$$

11)
$$8 + \underline{\hspace{1cm}} + 7 = 21$$

$$12) \ 9 \ + \ 4 \ + = 15$$

14)
$$46 = 29 + ___ + 12$$

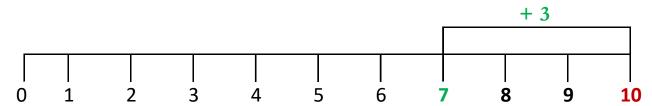
Find The Missing Number

1)
$$4 + ? = 7 + 3$$

Word Problem

- 4 + ? is equal to or the same value as 7 + 3
- or 7 + 3 is equal to or the same value as 4 + ?

Number Line



Step 1

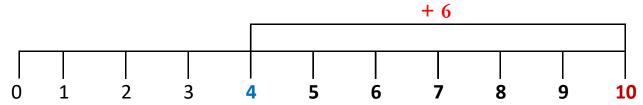
Out of the two **number sentences**, calculate the number sentence with all the **known** numbers first, which is 7 + 3.

First, find and touch the number seven on the number line.

Then, **count forwards three** more aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be **ten**.

Number Line



Step 2

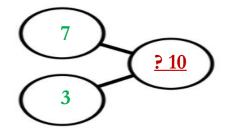
If 7 + 3 = 10, then 4 + ? = 10, as they are the same value. Secondly, find and touch the number four on a number line.

Then, from **four count forwards** aloud in number order, whilst touching the numbers on the number line, on to the number **ten**.

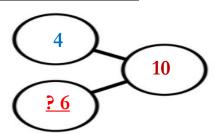
Next, say how many numbers were **counted on**, it should be **six** more.

Finally, the **value** of the missing number is **six**.

Part Whole Model



Part Whole Model



1)
$$4 + = 7 + 3$$

$$2)$$
 $7 + 2 = + 5$

$$5)$$
 ____ + 3 = 8 + 5

$$8) 12 + 4 = + 6$$

9)
$$1 + 14 = + 3$$

$$10) \ 16 + 2 = + 7$$

$$12)_{--} + 5 = 11 + 3$$

$$14)_{--} + 7 = 12 + 6$$

1 Less Than

Word Problem

Maja has two cubes.

How much is **one fewer?**

Concrete Object



Strategy Applied

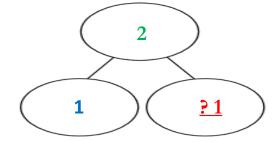
First, pick up **two** objects and place them together. Now count aloud to check there are only **two** objects; **one**, **two**.

Then, pick up one of the objects and take it away.

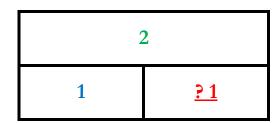
Next, count **altogether** how many objects are **left**. Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**.

Finally, two take away one equals one.

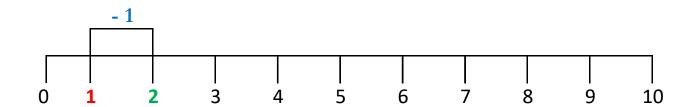
Part Whole Model



Bar Model



Number Line



Strategy Applied

First, find and touch the number two on the number line.

Then, **count backwards one** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be one.

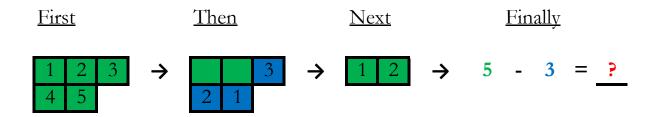
Finally, two subtract one equals one.

More Than 1

Word Problem

Ray has **five** pieces of fruit and he gives **three** pieces of fruit to Amy. How many pieces of fruit does he have **left?**

Concrete Object



Strategy Applied

First, pick up five objects and place them together.

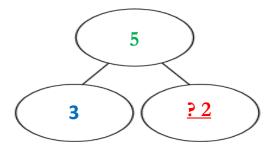
Now count aloud to check there are only **five** objects; **one**, **two**, **three**, **four**, **five**.

Then, pick up three of the objects and take them away.

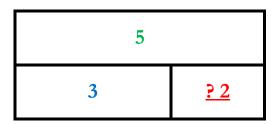
Next, count altogether how many objects are left.

Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**.

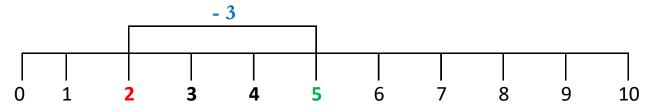
Finally, five take away three equals two.



Bar Model



Number Line



Strategy Applied

First, find and touch the number five on the number line.

Then, **count backwards three** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be two.

Finally, five subtract three equals two.

$$4) 8 - 5 =$$

10)
$$47m - 6m =$$

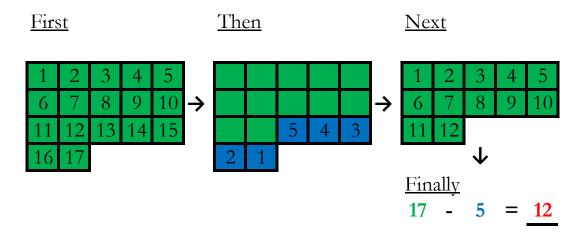
More Than 1

Word Problem

Mica and James have a maths problem to solve.

What is the **distance between seventeen** metres and **five** metres?

Concrete Object



Strategy Applied

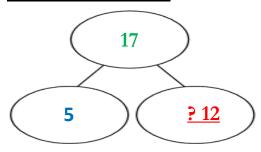
First, pick up seventeen objects and place them together.

Now count aloud to check there are only **seventeen** objects; 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17.

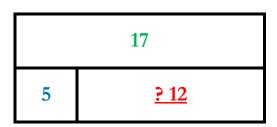
Then, pick up five of the objects and take them away.

Next, count **altogether** how many objects are **left**. Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**, **seven**, **eight**, **nine**, **ten**, **eleven**, **twelve**.

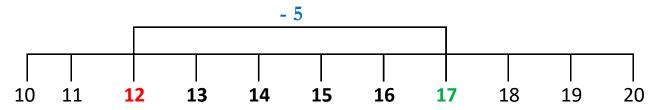
Finally, seventeen take away five equals twelve.



Bar Model



Number Line



Strategy Applied

First, find and touch the number seventeen on the number line.

Then, **count backwards five** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be **twelve**.

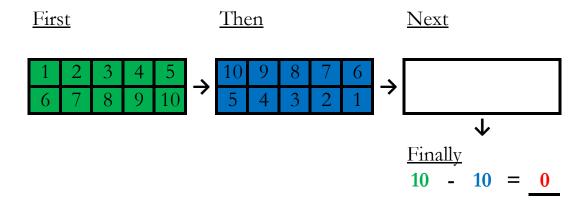
Finally, seventeen subtract five equals twelve.

10 Less Than

Word Problem

Josh has **ten** marbles and he gave all **ten** marbles to his friend Joseph. How many marbles does he have **left?**

Concrete Object



Strategy Applied

First, pick up ten objects and place them together.

Now count aloud to check there are only ten objects; 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.

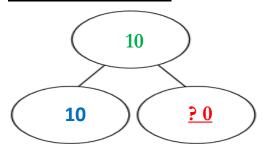
Then, pick up ten of the objects and take them away.

Next, count altogether how many objects are left.

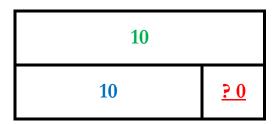
Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **zero**, as there are no objects left.

Finally, ten take away ten equals zero.

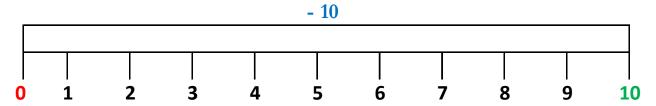
Part Whole Model



Bar Model



Number Line



Strategy Applied

First, find and touch the number ten on the number line.

Then, **count backwards ten** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be zero.

Finally, ten subtract ten equals zero.

8)
$$60g - 10g =$$

9)
$$80g - 10g =$$

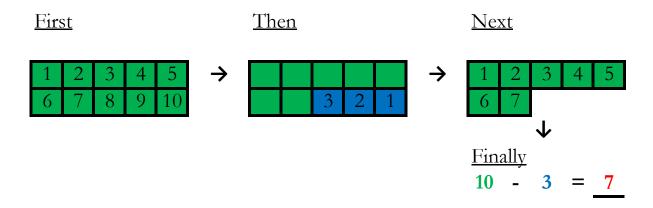
10)
$$100 \text{kg}$$
 - 10kg = ____

Bonds to 10 and 20

Number bonds to 10, means two or more numbers added together that make the number **10**.

Number bonds to 20, means two or more numbers added together that make the number 20.

Concrete Object



Strategy Applied

First, pick up ten objects and place them together.

Now count aloud to check there are only ten objects; 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.

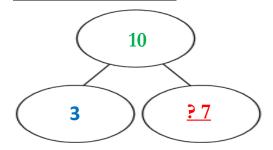
Then, pick up three of the objects and take them away.

Next, count altogether how many objects are left.

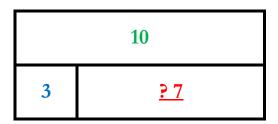
Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**, **five**, **six**, **seven**.

Finally, ten take away three equals seven.

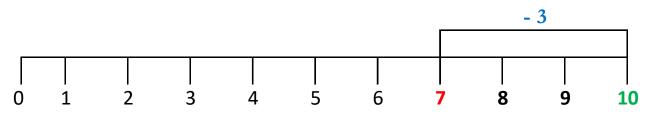
Part Whole Model



Bar Model



Number Line



Strategy Applied

First, find and touch the number ten on the number line.

Then, **count backwards three** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be seven.

Finally, ten subtract three equals seven.

6)
$$10p - \underline{\hspace{1cm}} = 4p$$

7)
$$20p - _ = 15p$$

8)
$$£20 - _{}$$
 = £17

5)
$$10p - _ = 2p$$

10)
$$£20$$
 - $£12$

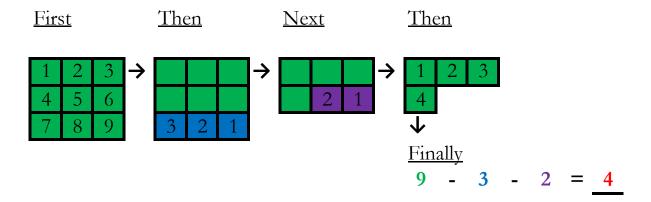
Multiple Numbers

Word Problem

There are **nine** apples in a basket. On Monday **three** apples are eaten. On Tuesday **two** more apples are eaten.

How many apples are left?

Concrete Object



Strategy Applied

First, pick up nine objects and place them together.

Now count aloud to check there are only nine objects; one, two, three, four, five, six, seven, eight, nine.

Then, pick up three of the objects and take them away.

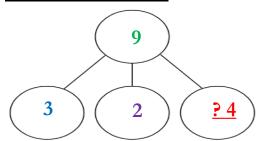
Next, pick up two more of the objects and take them away.

Then, count altogether how many objects are left.

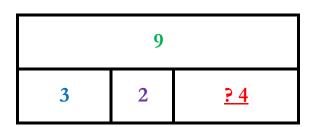
Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**, **two**, **three**, **four**.

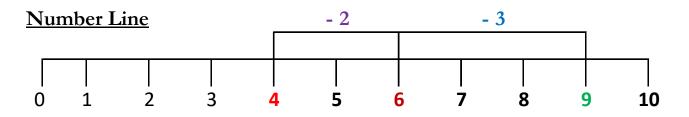
Finally, nine take away three take away two equals four.

Part Whole Model



Bar Model





Strategy Applied

First, find and touch the number nine on the number line.

Then, **count backwards three** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be six.

Then, **count backwards two** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted on to should be **four**.

Finally, nine subtract three subtract two equals four.

8)
$$40\text{ml}$$
 - 10ml - 10ml = ____

9)
$$60\text{ml}$$
 - 10ml - 10ml =

10)
$$100L - 10L - 10L =$$

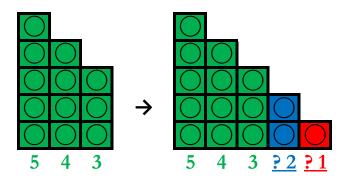
Multiples of 1, 2, 5 and 10

In the **number pattern** below, find the next two missing numbers.

Word Problem

The numbers **five**, **four** and **three** are written on part of a **number line**. Missing of the number line, are the **two** numbers written before. What are the **two** missing numbers?

Concrete Object



Strategy Applied

Work out the **number pattern**, by finding out the **difference between** the **three** numbers.

The difference between each of the three numbers is known as the rule.

First, **count backwards** from **five** to **four** equalling **one**, the rule is **-1**.

Then, count backwards from four to three equalling one, the rule is -1.

The rule is **-1**, **count back one** from each of the numbers in the number pattern.

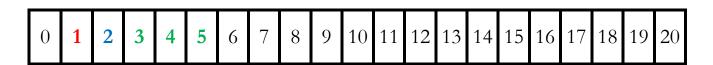
Continue this number pattern to find the next two missing numbers.

Next, find three on the number line and count back one less, total is two.

Then, find two on the number line and count back one less, total is one.

Finally, the next two missing numbers in the number pattern are two and one.

Number Line



Test Questions

In each **number pattern**, find the next two missing numbers.

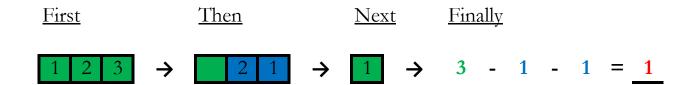
Doubling

Word Problem

There are **three** oranges in a bowl. On Wednesday **one** orange is eaten. On Thursday **one further** orange is eaten.

How many oranges are left?

Concrete Object



Strategy Applied

First, pick up three objects and place them together.

Now count aloud to check there are only three objects; one, two, three.

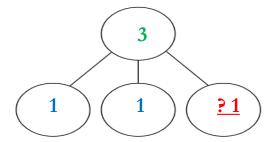
Then, pick up one and one of the objects equal to two objects and take them away.

Next, count altogether how many objects are left.

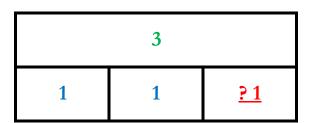
Whilst touching each object **count forwards** aloud in number order, saying one number name per object; **one**.

Finally, three take away double one equals one.

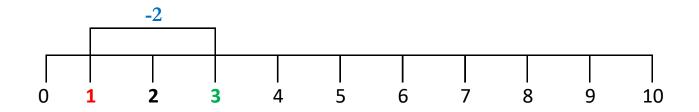
Part Whole Model



Bar Model



Number Line



Strategy Applied

First, find and touch the number three on the number line.

Then, **count backwards two** less (double **one**) aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be **one**.

Finally, three take away double one equals one.

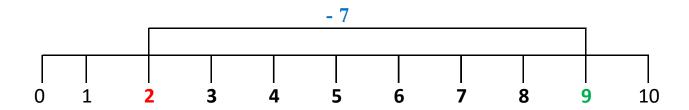
Find The Missing Number

Word Problem

Nine children are sat down at a table eating their lunch. A number of the children finish their lunch and go out to play. Two children are still sat at the table eating their lunch.

How many of the children went out to play?

Number Line



Strategy Applied

First, find and touch the number nine on the number line.

Then, **count backwards seven** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be two.

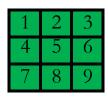
Finally, nine subtract seven equals two.

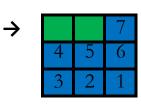
Concrete Object

<u>First</u>

<u>Then</u>

Next Finally

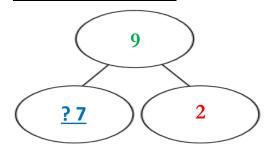




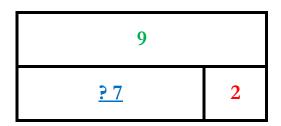
 \rightarrow



Part Whole Model



Bar Model



$$2) \quad 6 \quad - \quad = \quad 6$$

$$3) 10 - = 2$$

4)
$$10 - = 10$$

$$7) 26 - = 6$$

$$9) - 2 = 7$$

$$10) - 4 = 6$$

$$11) - 10 = 7$$

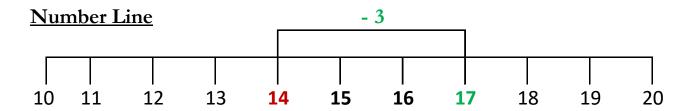
$$13) - 40 = 7$$

Find The Missing Number

1)
$$17 - 3 = ? - 2$$

Word Problem

- 17 3 is equal to or the same value as ? 2
- or ? 2 is equal to or the same value as 17 3



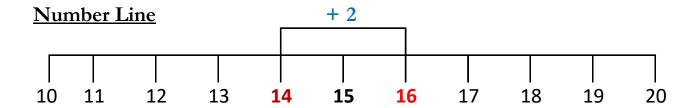
Step 1

Out of the two **number sentences**, calculate the number sentence with all the **known** numbers first which is, 17 - 3.

First, find and touch the number seventeen on the number line.

Then, **count backwards three** less aloud in number order, whilst touching the numbers on the number line.

Next, the number counted back to should be **fourteen**.



Step 2

If 17 - 3 = 14, then ? - 2 = 14, as they are the same value. Use the inverse of subtraction, which is addition, 14 + 2 = ?.

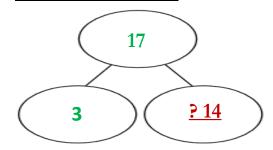
Secondly, find and touch the number fourteen on a number line.

Then, **count forwards one** more aloud in number order, whilst touching the numbers on the number line.

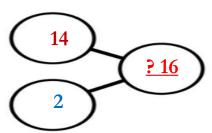
Next, the number counted on to should be sixteen.

Finally, the value of the missing number is sixteen.

Part Whole Model



Part Whole Model



1)
$$17 - 3 = -2$$

$$3)$$
 18 - = 6 + 5

$$5) 19 - = 6 + 5$$

7)
$$18 - _ _ - 4 = 12$$

10)
$$27 - 6 + 5 =$$

11) 24 -
$$+$$
 7 = 17

13)
$$45 - 6 - = 31$$

14)
$$70 - 10 + 10 + 10 =$$

Repeated Addition

1)
$$2 \times 3 = ?$$

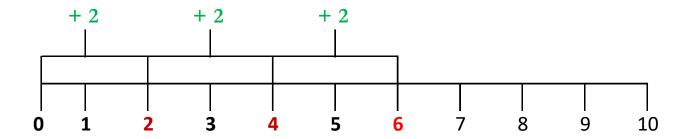
Word Problem

Sam has three groups of two cubes.

Sam has **two** cubes, then **adds two** more cubes, then **adds two** more cubes, **repeated addition.**

How many cubes does Sam have altogether?

Number Line



Strategy Applied

First, find and touch the number zero on a number line.

Then, **count forwards two** more aloud in number order, whilst touching the numbers on the number line, on to the number **two**.

Next, **count forwards two** more aloud in number order, whilst touching the numbers on the number line, on to the number **four**.

Then, **count forwards two** more aloud in number order, whilst touching the numbers on the number line, on to the number **six**.

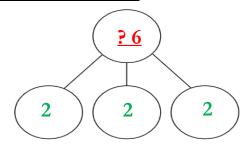
Finally, two times three equals six.

Concrete Object

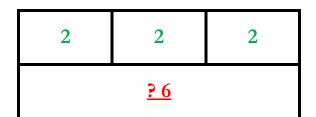
$$2 + 2 + 2 = \frac{?6}{}$$

Column Addition

Part Whole Model



Bar Model



$$5) \quad 5 \quad x \quad 3 =$$

6) 5
$$x$$
 4 = ____

7) 5
$$x$$
 6 = ____

8)
$$10 \times 2 =$$

9)
$$10 \times 3 =$$

10) 10
$$\times$$
 5 =

11)
$$= 2 \times 7$$

$$12) = 2 \times 9$$

13)
$$= 5 \times 8$$

$$14) = 10 \times 8$$

Repeated Subtraction

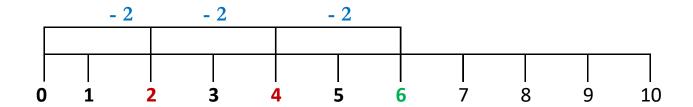
1)
$$6 \div 2 = ?$$

Word Problem

Six toys are equally shared between two groups of children.

How many toys will each group have?

Number Line



Strategy Applied

First, find and touch the number six on a number line.

Then, **count backwards two** less aloud in number order, whilst touching the numbers on the number line, back to the number **four**.

Next, **count backwards two** less aloud in number order, whilst touching the numbers on the number line, back to the number **two**.

Then, **count backwards two** less aloud in number order, whilst touching the numbers on the number line, back to the number **zero**.

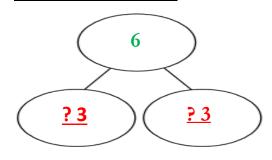
Finally, six divided by two equals three.

Concrete Object

Quantity

Group 1 Group 2

Part Whole Model



Bar Model

(6
<u>? 3</u>	<u>? 3</u>

4)
$$12 \div 2 =$$

6)
$$10 \div 5 =$$

8)
$$20 \div 5 =$$

10) 50
$$\div$$
 10 =

$$11) = 16 \div 2$$

$$12) = 24 \div 2$$

$$13) = 40 \div 5$$

$$14) = 80 \div 10$$

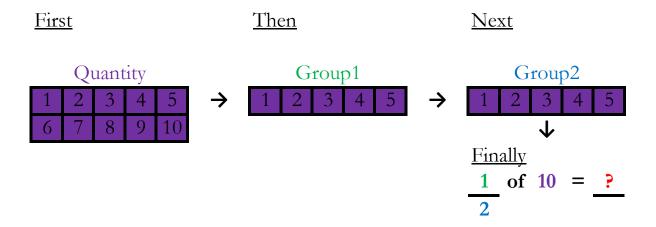
Fraction of a Quantity

1)
$$\frac{1}{2}$$
 of 10 = $\frac{?}{}$

Word Problem

Lacey and Vanessa **equally** share **ten** cubes between the **two** of them. How many cubes will **one** of them have?

Concrete Object



Strategy Applied

A fraction is part of a whole or part of 1 and a half is 1 of 2 equal groups.

10 is the quantity shared equally between the total number of equal groups.

- 2 is the **denominator**, represents the **total** number of **equal groups**.
- 1 is the numerator, represents one of the equal groups.

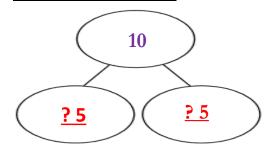
First, pick up ten objects and place them together. Now count aloud to check there are only ten objects; 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.

Then, share the ten objects one at a time equally between the two groups, until exactly the same quantity of objects are in each of the groups.

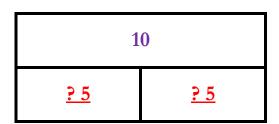
Next, count how many objects there are altogether in one group, there should be five objects; one, two, three, four, five.

Finally, one half of ten equals five.

Part Whole Model



Bar Model



1)
$$\frac{1}{2}$$
 of 10 = ____

2)
$$\frac{1}{4}$$
 of 12 = ____

3)
$$\frac{1}{4}$$
 of 20 = ____

4) A half of
$$4 = \underline{}$$

7) ___ =
$$\frac{1}{2}$$
 of 20g

8) ___ =
$$\frac{1}{2}$$
 of 14kg

9) ___ =
$$\frac{1}{4}$$
 of 16ml

10) =
$$\frac{1}{4}$$
 of 24L

Answers

<u>P. 2</u>	<u>P. 4</u>	<u>P. 6</u>	<u>P. 8</u>
1) 1 ten and 4 ones	1) 10 + 4	1) 2	1) 8
2) 1 ten and 5 ones	2) 10 + 5	2) 5	2) 10
3) 1 ten and 7 ones	3) 10 + 7	3) 7	3) 14
4) 1 ten and 9 ones	4) 10 + 9	4) 6	4) 15
5) 2 tens and 0 ones	5) 20 + 0	5) 9	5) 14mm
6) 2 tens and 3 ones	6) 20 + 3	6) 6	6) 8
7) 3 tens and 0 ones	$7) \ 30 + 0$	7) 11	7) 19cm
8) 4 tens and 5 ones	8) 40 + 5	8) 4mm	8) 19m
9) 5 tens and 7 ones	9) $50 + 7$	9) 28cm	9) 18
10) 6 tens and 9 ones	10) 60 + 9	10) 44m	10) 19
11) 7 tens and 0 ones	11) $70 + 0$		
12) 8 tens and 3 ones	12) 80 + 3		
13) 9 tens and 4 ones	13) 90 + 4		
14) 9 tens and 9 ones	14) 90 + 9		

<u>P. 10</u>	<u>P. 12</u>	<u>P. 14</u>	<u>P. 16</u>	<u>P. 18</u>
1) 2	1) 20	1) 10	1) 6	1) 5, 6
2) 2	2) 11	2) 7	2) 9	2) 8, 9
3) 5	3) 40	3) 5	3) 17	3) 17, 18
4) 2	4) 70	4) 3	4) 14	4) 23, 24
5) 4	5) 60	5) 2p	5) 20	5) 6, 8
6) 2	6) 50	6) 4p	6) 30	6) 16, 18
7) 8	7) 80	7) £6	7) 40	7) 26, 28
8) 8ml	8) 30g	8) £8	8) 50secs	8) 38, 40
9) 16ml	9) 100g	9) 20	9) 70secs	9) 15, 20
10) 16L	10) 110kg	10) 12	10) 100mins	10) 30, 35

Answers

<u>P. 20</u>	<u>P. 22</u>	<u>P. 24</u>	<u>P. 26</u>	<u>P. 28</u>	<u>P. 30</u>
1) 4	1) 2	1) 6	1) 1	1) 2	1) 12
2) 8	2) 6	2) 4	2) 2	2) 2	2) 9
3) 12	3) 6	3) 10	3) 7	3) 7	3) 8secs
4) 2	4) 4	4) 9	4) 4	4) 3	4) 8secs
5) 6	5) 7	5) 10	5) 8	5) 9	5) 1mins
6) 10	6) 6	6) 5	6) 4	6) 6	6) 9
7) 16	7) 3	7) 10	7) 13	7) 13	7) 12mins
8) 20	8) 5	8) 10	8) 3mm	8) 18mm	8) 13hrs
9) 0	9) 9	9) 12	9) 5cm	9) 25cm	9) 7hrs
10) 22	10) 6	10) 11	10) 8m	10) 41m	10) 11

<u>P. 32</u>	<u>P. 34</u>	<u>P. 36</u>	<u>P. 38</u>	<u>P. 40</u>	<u>P. 42</u>
1) 0	1) 7	1) 4	1) 2, 1	1) 1	1) 7
2) 20	2) 4	2) 5	2) 7, 6	2) 2	2) 0
3) 40	3) 2	3) 4	3) 5, 4	3) 1	3) 8
4) 60	4) 9	4) 11	4) 16, 15	4) 2	4) 0
5) 80	5) 8p	5) 10	5) 4, 2	5) 3	5) 5
6) 10	6) 6p	6) 10	6) 6, 4	6) 2	6) 10
7) 30	7) 5p	7) 30	7) 14, 12	7) 3	7) 20
8) 50g	8) £3	8) 20ml	8) 24, 22	8) 4	8) 20
9) 70g	9) £16	9) 40ml	9) 10, 5	9) 3	9) 9
10) 90kg	10) £8	10) 80L	10) 15, 10	10) 4	10) 10
				11) 3	11) 17
				12) 5	12) 20
				13) 8	13) 47
				14) 10	14) 50

Answers

<u>P. 44</u>	<u>P. 46</u>	<u>P. 48</u>	<u>P. 50</u>
1) 16	1) 6	1) 3	1) 5
2) 19	2) 8	2) 4	2) 3
3) 7	3) 10	3) 5	3) 5
4) 9	4) 16	4) 6	4) 2
5) 8	5) 15	5) 9	5) 1
6) 3	6) 20	6) 2	6) 10
7) 2	7) 30	7) 3	7) 10g
8) 5	8) 20	8) 4	8) 7kg
9) 6	9) 30	9) 3	9) 4ml
10) 16	10) 50	10) 5	10) 6L
11) 0	11) 14	11) 8	
12) 0	12) 18	12) 12	
13) 8	13) 40	13) 8	
14) 40	14) 80	14) 8	

Amount is something that has a numerical value, for e.g. 10 cubes

Bar Model is a pictorial representation of a number sentence in the form of bars or boxes used to solve number problems.

Column is a vertical arrangement for example, in a table the cells arranged vertically.

Column Place Value is the value of a digit that relates to its position or place in a number within a column.

Concrete Objects are objects that can be handled and manipulated to support understanding of the structure of a mathematical concept. Materials such as Dienes(Base 10 materials), Cuisenaire, Numicon, are all examples of concrete objects.

Denominator is the number written below the line i.e. the divisor. e.g. in the fraction ²/₃ the denominator is 3.

Digit is one of the symbols of a number system most commonly the symbols 0, 1, 2, 3, 4, 5, 6, 7, 8 and 9. Examples: the number 29 is a 2-digit number; there are three digits in 2.95. The position or place of a digit in a number conveys its value.

Digit Value is the value of a digit that relates to its position or place in a number. e.g. in 82 the digits represent 8 tens and 2 ones.

Dividend in division, is the number that is divided. e.g. in $15 \div 3$, 15 is the dividend.

Divisor is the number by which another is divided. e.g. In the calculation $30 \div 6 = 5$, the divisor is 6. In this example, 30 is the dividend and 5 is the quotient.

Efficient Methods A means of calculation (which can be mental or written) that achieves a correct answer with as few steps as possible. In written calculations this often involves setting out calculations in a columnar layout.

Equals is the symbol: =, read as 'is equal to' or 'equals'. and meaning 'having the same value as'. e.g. 7 - 2 = 4 + 1 since both expressions, 7 - 2 and 4 + 1 have the same value, 5.

Expanded Form is a way to break up a number to show the value of each digit (Partition).

Fraction is the result of dividing one integer by a second integer, which must be non-zero. The dividend is the numerator and the non-zero divisor is the denominator. See also decimal fraction, equivalent fraction, improper fraction, proper fraction, unit fraction and vulgar fraction.

Formal Written Method is the way of setting out working in columnar form. In addition and subtraction, the formal written methods can be referred to as expanded and column addition and/or subtraction. In multiplication, the formal written methods are called short or long multiplication depending on the size of the numbers involved. Similarly in division the formal written methods are called short or long division.

Grid a lattice created with two sets of parallel lines. Lines in each set are usually equally spaced. If the sets of lines are at right angles and lines in both sets are equally spaced, a square grid is created.

Hundred Square is a 10 by 10 square grid numbered 1 to 100. A similar grid could be numbered as a 0 - 99 grid.

Inverse is the opposite or reverse operation.

Mental Calculations refer to calculations that are largely carried out mentally, but may be supported with a few simple written jottings.

Multiple is the result of multiplying a number by an integer, e.g. 12 is a multiple of 3 because $3 \times 4 = 12$.

Multiplicand is a number to be multiplied by another. e.g. in 6×4 , 4 is the multiplier as it is how many lots/groups of 6.

Multiplier is a number to be multiplied by another. e.g. in 5×3 , 5 is the multiplicand as it is the number to be multiplied by 3.

Number Bond is a pair of numbers with a particular total.

Number Line is a line where numbers are represented by points upon it.

Number Sentence is a mathematical sentence involving numbers. e.g. 3 + 6 = 9 and 9 > 3

Numerator is the number written on the top—the dividend (the part that is divided). In the fraction ²/₃, the numerator is 2.

Operations that, when they are combined, leave the entity on which they operate unchanged. Examples: addition and subtraction are inverse operations e.g. 5 + 6 - 6 = 5. Multiplication and division are inverse operations e.g. $6 \times 10 \div 10 = 6$.

Part Whole Model is a pictorial representation of the relationship between a number or number sentence and its component parts.

Partition 1) To separate a set into subsets. 2) To split a number into component parts. e.g. the two-digit number 38 can be partitioned into 30 + 8 or 19 + 19. 3) A model of division. e.g. $21 \div 7$ is treated as 'how many sevens in 21?'

Pictorial Representations do enable learners to use pictures and images to represent the structure of a mathematical concept.

The pictorial representation may build on the familiarity with concrete objects. e.g. a square to represent a Dienes 'flat' (representing 100). Pupils may interpret pictorial representations provided to them or create a pictorial representation themselves to help solve a mathematical problem.

Place Holder In decimal notation, the zero numeral is used as a place holder to denote the absence of a power of 10.

Place Value is the value of a digit that relates to its position or place in a number. e.g. in 1482 the digits represent 1 thousand, 4 hundred, 8 tens and 2 ones respectively; in 12.34 the digits represent 1 ten, 2 ones, 3 tenths and 4 hundredths respectively.

Product is the result of multiplying one number by another. e.g. the product of 2 and 3 is 6 since $2 \times 3 = 6$.

Quotient is the result of a division. e.g. $46 \div 3 = 15\frac{1}{3}$ and $15\frac{1}{3}$ is the quotient of 46 by 3. Where the operation of division is applied to the set of integers, and the result expressed in integers.

e.g. $46 \div 3 = 15$ remainder 1 then 15 is the quotient of 46 by 3 and 1 is the remainder.

Regrouping is to exchange a number for another of equal value. The process of regrouping is used in some standard compact methods of calculation. e.g.: 'carrying figures/exchanging' in addition, multiplication or division; and 'decomposition' in subtraction.

Remainder in the context of division requiring a whole number answer (quotient), the amount remaining after the operation. e.g. 29 divided by 7 = 4 remainder 1.

Repeated Addition is the process of repeatedly adding the same number or amount. One model for multiplication. e.g. $5 + 5 + 5 + 5 = 5 \times 4$.

Repeated Subtraction is The process of repeatedly subtracting the same number or amount. One model for division.

e.g. 20 - 5 - 5 - 5 - 5 = 0 so $20 \div 4 = 5$ remainder 0.

Sequence is succession of terms formed according to a rule. There is a definite relation between one term and the next and between each term and its position in the sequence. e.g. 0, 4, 8, 12, 16 etc.

Step Counting is the process of repeatedly adding the same number or amount. One model for multiplication. e.g. $5 + 10 + 15 + 20 = 5 \times 4$.

Total Value is the sum to a calculation.

Zero in a place value system, a place-holder. e.g. 105